

From Collinear to TMD Distributions in the Large- x Regime

JHEP 06 (2025) 218 (O. Del Rio, A. Prokudin, I. Scimemi and A. Vladimirov)

QCD Evolution 2026

Óscar del Río García. May 13th 2026



PID2022-136510NB-C31



UNIVERSIDAD
COMPLUTENSE
MADRID



Distribution Functions for Partons

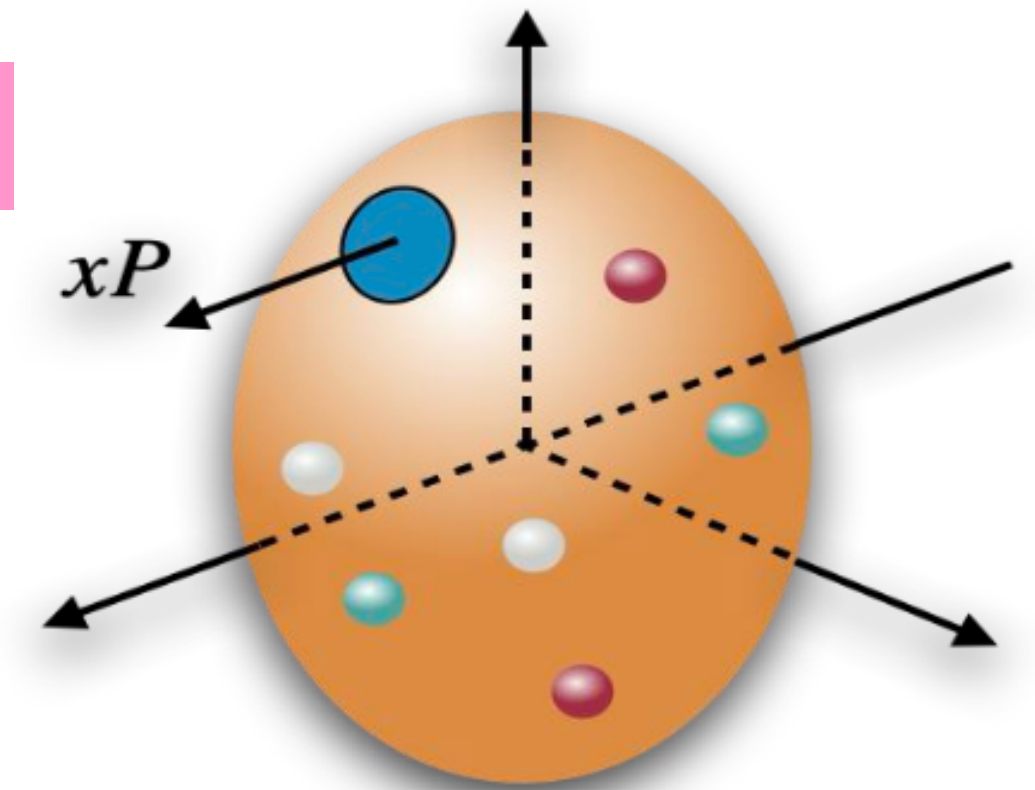
- Twist-2 quark **PDF** operator definition

Twist \equiv Dimension – Spin = 2

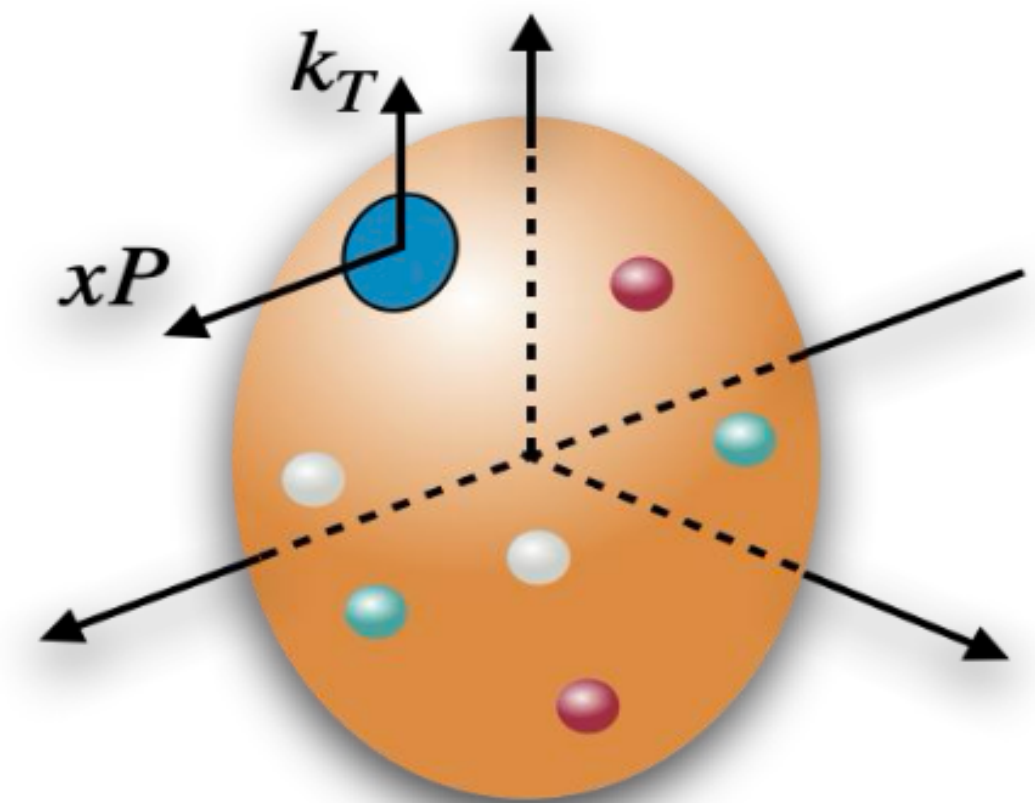
$$f^{[\Gamma]}(x) = \int \frac{db^+}{2\pi} e^{-ib^+(xP^-)} \langle P, S | \bar{q}(b^+) [b^+, 0] \Gamma q(0) | P, S \rangle$$

- Twist-2 quark **TMDPDF** operator definition

$$F^{[\Gamma]}(x, b_T) = \int \frac{db^+}{2\pi} e^{-ib^+(xP^-)} \langle P, S | \bar{q}(b) [b, b + s\infty][b + s\infty, s\infty][s\infty, 0] \Gamma q(0) | P, S \rangle$$



PDF



TMD

Distribution Functions for Partons

- Twist-2 quark **PDF** operator definition

$$\text{Twist} \equiv \text{Dimension} - \text{Spin} = 2$$

$$f^{[\Gamma]}(x) = \int \frac{db^+}{2\pi} e^{-ib^+(xP^-)} \langle P, S | \bar{q}(b^+) [b^+, 0] \Gamma q(0) | P, S \rangle$$

- Twist-2 quark **TMDPDF** operator definition

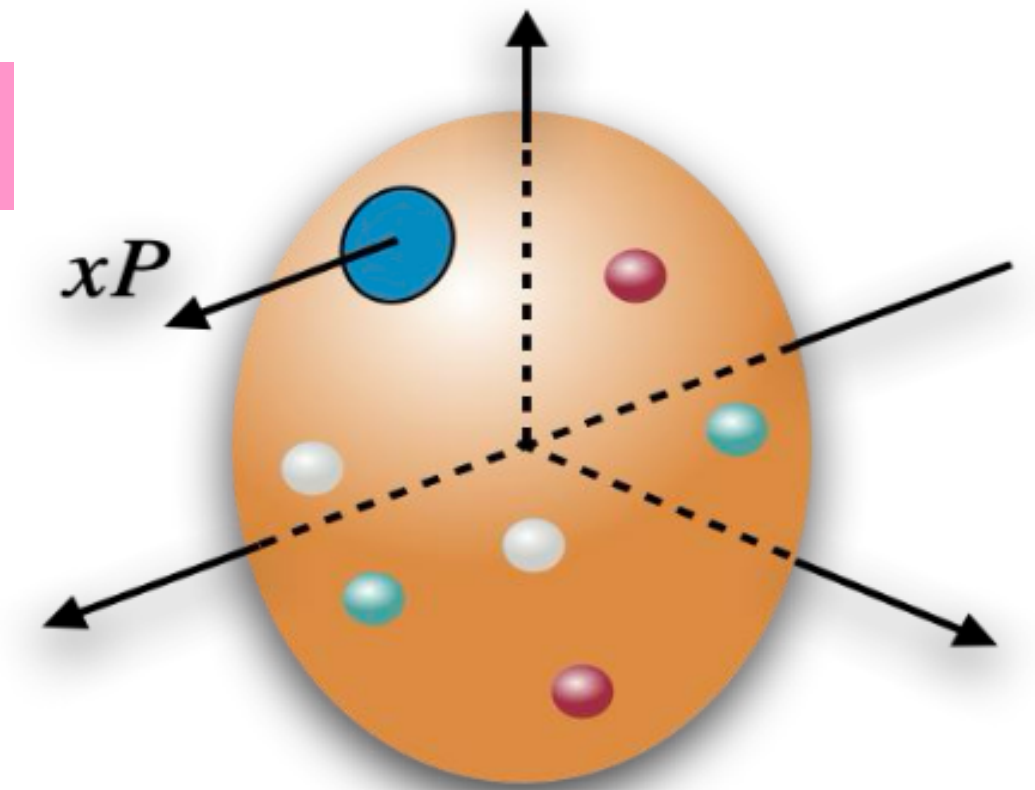
$$F^{[\Gamma]}(x, b_T) = \int \frac{db^+}{2\pi} e^{-ib^+(xP^-)} \langle P, S | \bar{q}(b) [b, b + s\infty][b + s\infty, s\infty][s\infty, 0] \Gamma q(0) | P, S \rangle$$

- Higher twist operators involve more fields:

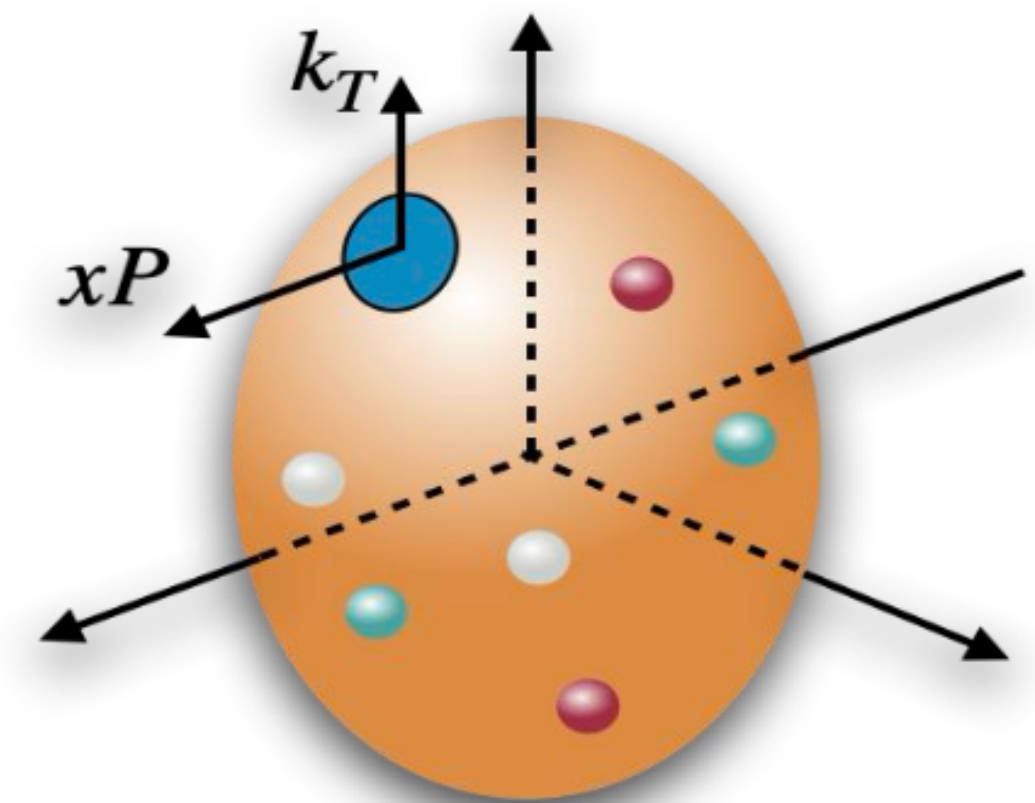
$$\langle P, S | \bar{q}(b_1^+) [b_1^+, b_2^+] \Gamma F^{\mu+}(b_2^+) [b_2^+, b_3^+] q(b_3^+) | P, S \rangle$$

$$\langle P, S | F^{\mu+}(b_1^+) [b_1^+, b_2^+] \Gamma F^{\nu+}(b_2^+) [b_2^+, b_3^+] F^{\rho+}(b_3^+) | P, S \rangle$$

$$\text{Twist} = 3$$



PDF



TMD

Distribution Functions for Partons

- Three independent twist-2 quark PDFs:

$\Gamma = \gamma^+$	$\Gamma = \gamma^+\gamma^5$	$\Gamma = i\sigma^{\nu+}\gamma^5$
$f_1(x)$ Unpolarized	$g_1(x)$ Helicity	$h_1(x)$ Transversity

- Eight independent twist-2 quark TMDPDFs:

$\Gamma = \gamma^+$	$\Gamma = \gamma^+\gamma^5$	$\Gamma = i\sigma^{\nu+}\gamma^5$	
$f_1(x, b_T)$ Unpolarized	$g_1(x, b_T)$ Helicity	$h_1(x, b_T)$ Transversity	$h_1^\perp(x, b_T)$ Boer-Mulders
$f_{1T}^\perp(x, b_T)$ Sivers	$g_{1T}^\perp(x, b_T)$ Worm-gear-T	$h_{1L}^\perp(x, b_T)$ Worm-gear-L	$h_{1T}^\perp(x, b_T)$ Pretzelosity

Distribution Functions for Partons

- Three independent twist-2 quark PDFs:

$\Gamma = \gamma^+$	$\Gamma = \gamma^+\gamma^5$	$\Gamma = i\sigma^{\nu+}\gamma^5$
$f_1(x)$ Unpolarized	$g_1(x)$ Helicity	$h_1(x)$ Transversity

- Eight independent twist-2 quark TMDPDFs:

$\Gamma = \gamma^+$	$\Gamma = \gamma^+\gamma^5$	$\Gamma = i\sigma^{\nu+}\gamma^5$	
$f_1(x, b_T)$ Unpolarized	$g_1(x, b_T)$ Helicity	$h_1(x, b_T)$ Transversity	$h_1^\perp(x, b_T)$ Boer-Mulders
$f_{1T}^\perp(x, b_T)$ Sivers	$g_{1T}^\perp(x, b_T)$ Worm-gear-T	$h_{1L}^\perp(x, b_T)$ Worm-gear-L	$h_{1T}^\perp(x, b_T)$ Pretzelosity

- Twist-3 PDFs (arxiv: 2209.00962)
 - ▶ $\bar{q}F^{\mu+}q \longrightarrow T(x_1, x_2, x_3) \quad \Delta T(x_1, x_2, x_3) \quad E(x_1, x_2, x_3) \quad H(x_1, x_2, x_3)$
 - ▶ $F^{\mu+} \times 3 \longrightarrow G_\pm(x_1, x_2, x_3) \quad Y_\pm(x_1, x_2, x_3)$

Matching Coefficient Function

- Related by **Operator Product Expansion** in small b_T regime

$$F_i(x, b_T) = \underbrace{C_{ij}^F(x, b_T)}_{\substack{\text{Twist-2} \\ \text{Match.} \\ \text{Coeff.}}} \otimes f_j(x) + \sum_t \underbrace{C_{t,ij}^F(x, x_1, x_2, x_3, b_T)}_{\substack{\text{Twist-3 Matching} \\ \text{Coefficient}}} \otimes t_j(x_1, x_2, x_3) + \mathcal{O}(b_T^2)$$

Matching Coefficient Function

- Related by **Operator Product Expansion** in small b_T regime

$$F_i(x, b_T) = \underbrace{C_{ij}^F(x, b_T)}_{\substack{\text{Twist-2} \\ \text{Match.} \\ \text{Coeff.}}} \otimes f_j(x) + \sum_t \underbrace{C_{t,ij}^F(x, x_1, x_2, x_3, b_T)}_{\substack{\text{Twist-3 Matching} \\ \text{Coefficient}}} \otimes t_j(x_1, x_2, x_3) + \mathcal{O}(b_T^2)$$

TMDPDF	Leading Matching PDFs	Order Matching Coeff.
Unpolarized $f_1(x, b_T)$	$f_1(x)$	N ³ LO
Helicity $g_1(x, b_T)$	$g_1(x)$	NLO
Transversity $h_1(x, b_T)$	$h_1(x)$	N ² LO

} Twist-2

Matching Coefficient Function

- Related by **Operator Product Expansion** in small b_T regime

$$F_i(x, b_T) = \underbrace{C_{ij}^F(x, b_T)}_{\substack{\text{Twist-2} \\ \text{Match.} \\ \text{Coeff.}}} \otimes f_j(x) + \sum_t \underbrace{C_{t,ij}^F(x, x_1, x_2, x_3, b_T)}_{\substack{\text{Twist-3 Matching} \\ \text{Coefficient}}} \otimes t_j(x_1, x_2, x_3) + \mathcal{O}(b_T^2)$$

TMDPDF	Leading Matching PDFs	Order Matching Coeff.
Unpolarized $f_1(x, b_T)$	$f_1(x)$	N ³ LO
Helicity $g_1(x, b_T)$	$g_1(x)$	NLO
Transversity $h_1(x, b_T)$	$h_1(x)$	N ² LO
Worm-gear-L $h_{1L}^\perp(x, b_T)$	h_1, E, H	NLO
Worm-gear-T $g_{1T}^\perp(x, b_T)$	$g_1, T, \Delta T, G_\pm, Y_\pm$	NLO

} Twist-2
 } Twist-2&3

Matching Coefficient Function

- Related by **Operator Product Expansion** in small b_T regime

$$F_i(x, b_T) = \underbrace{C_{ij}^F(x, b_T)}_{\text{Twist-2 Match. Coeff.}} \otimes f_j(x) + \sum_t \underbrace{C_{t,ij}^F(x, x_1, x_2, x_3, b_T)}_{\text{Twist-3 Matching Coefficient}} \otimes t_j(x_1, x_2, x_3) + \mathcal{O}(b_T^2)$$

TMDPDF	Leading Matching PDFs	Order Matching Coeff.
Unpolarized $f_1(x, b_T)$	$f_1(x)$	N ³ LO
Helicity $g_1(x, b_T)$	$g_1(x)$	NLO
Transversity $h_1(x, b_T)$	$h_1(x)$	N ² LO
Worm-gear-L $h_{1L}^\perp(x, b_T)$	Wandzura-Wilczek h_1 E, H	NLO
Worm-gear-T $g_{1T}^\perp(x, b_T)$	Contributions g_1 $T, \Delta T, G_\pm, Y_\pm$	NLO

} Twist-2
 } Twist-2&3

Matching Coefficient Function

- Related by **Operator Product Expansion** in small b_T regime

$$F_i(x, b_T) = \underbrace{C_{ij}^F(x, b_T)}_{\substack{\text{Twist-2} \\ \text{Match.} \\ \text{Coeff.}}} \otimes f_j(x) + \sum_t \underbrace{C_{t,ij}^F(x, x_1, x_2, x_3, b_T)}_{\substack{\text{Twist-3 Matching} \\ \text{Coefficient}}} \otimes t_j(x_1, x_2, x_3) + \mathcal{O}(b_T^2)$$

TMDPDF	Leading Matching PDFs	Order Matching Coeff.
Unpolarized $f_1(x, b_T)$	$f_1(x)$	N ³ LO
Helicity $g_1(x, b_T)$	$g_1(x)$	NLO
Transversity $h_1(x, b_T)$	$h_1(x)$	N ² LO
Worm-gear-L $h_{1L}^\perp(x, b_T)$	Wandzura-Wilczek h_1 E, H	NLO
Worm-gear-T $g_{1T}^\perp(x, b_T)$	Contributions g_1 $T, \Delta T, G_\pm, Y_\pm$	NLO
Sivers $f_{1T}^\perp(x, b_T)$	$T, \Delta T, G_\pm, Y_\pm$	NLO
Boer-Mulders $h_1^\perp(x, b_T)$	$E(x_1, x_2, x_3)$	NLO
Pretzelosity $h_{1T}^\perp(x, b_T)$	—	-

} Twist-2
} Twist-2&3
} Twist-3
} Twist-4

Matching Coefficient Function at Large- x

- Three type of contributions to $C^F(x, b_T)$:

▶ Harmonic Polylogarithms $\rightarrow H(a_1, \dots, a_n, x)$ ▶ Delta Distribution $\rightarrow L_0(x) = \delta(1 - x)$

▶ Plus Distributions $\rightarrow L_1(x) = \frac{1}{(1-x)_+}$, ..., $L_m(x) = \left(\frac{\ln^{m-1}(1-x)}{1-x} \right)_+$

Singular $x \rightarrow 1$
(Dominate at large- x)

Matching Coefficient Function at Large- x

- Three type of contributions to $C^F(x, b_T)$:

▶ Harmonic Polylogarithms $\rightarrow H(a_1, \dots, a_n, x)$ ▶ Delta Distribution $\rightarrow L_0(x) = \delta(1 - x)$

▶ Plus Distributions $\rightarrow L_1(x) = \frac{1}{(1-x)_+}, \dots, L_m(x) = \left(\frac{\ln^{m-1}(1-x)}{1-x} \right)_+$

Singular $x \rightarrow 1$
(Dominate at large- x)

- Expansion in loops (α_s^n) and in L_m

$$C^F = \sum_{n,m} \alpha_s^n [L_m C_{n,m}^F + \Delta C_n^F] = \begin{array}{l} \boxed{L_0 C_{0,0}^F} \quad \text{LO} \\ \boxed{+\alpha_s L_1 C_{1,1}^F + \alpha_s L_0 C_{1,0}^F} \quad +\alpha_s \Delta C_1^F \quad \text{NLO} \\ \boxed{+\alpha_s^2 L_2 C_{2,2}^F + \alpha_s^2 L_1 C_{2,1}^F + \alpha_s^2 L_0 C_{2,0}^F} \quad +\alpha_s^2 \Delta C_2^F \quad \text{N}^2\text{LO} \\ + \dots \quad \vdots \end{array}$$

Matching Coefficient Function at Large- x

- Three type of contributions to $C^F(x, b_T)$:

▶ Harmonic Polylogarithms $\rightarrow H(a_1, \dots, a_n, x)$ ▶ Delta Distribution $\rightarrow L_0(x) = \delta(1 - x)$

▶ Plus Distributions $\rightarrow L_1(x) = \frac{1}{(1-x)_+}, \dots, L_m(x) = \left(\frac{\ln^{m-1}(1-x)}{1-x} \right)_+$

Singular $x \rightarrow 1$
(Dominate at large- x)

- Expansion in loops (α_s^n) and in L_m

$$C^F = \sum_{n,m} \alpha_s^n [L_m C_{n,m}^F + \Delta C_n^F] = \begin{matrix} L_0 C_{0,0}^F \\ + \alpha_s L_1 C_{1,1}^F + \alpha_s L_0 C_{1,0}^F \\ + \alpha_s^2 L_2 C_{2,2}^F + \alpha_s^2 L_1 C_{2,1}^F + \alpha_s^2 L_0 C_{2,0}^F \\ \dots \end{matrix} \begin{matrix} \\ + \alpha_s \Delta C_1^F \\ + \alpha_s^2 \Delta C_2^F \\ \dots \end{matrix}$$

LL_x
NLL_x
N²LL_x
...

Matching Coefficient Function in Mellin Space

- Mellin transformation

$$\mathbf{M}_N[C^F] = \int_0^1 dx x^{N-1} C^F(x, b_T)$$

- Large- x asymptotics correspond to large- N dominant terms in Mellin space

$$\lim_{N \rightarrow \infty} \mathbf{M}_N[H] = 0$$

$$\lim_{N \rightarrow \infty} \mathbf{M}_N[L_0] = 1$$

$$\lim_{N \rightarrow \infty} \mathbf{M}_N[L_m] \sim \ln^m N$$

Matching Coefficient Function in Mellin Space

- Mellin transformation

$$\mathbf{M}_N[C^F] = \int_0^1 dx x^{N-1} C^F(x, b_T)$$

- Large- x asymptotics correspond to large- N dominant terms in Mellin space

$$\lim_{N \rightarrow \infty} \mathbf{M}_N[H] = 0$$

$$\lim_{N \rightarrow \infty} \mathbf{M}_N[L_0] = 1$$

$$\lim_{N \rightarrow \infty} \mathbf{M}_N[L_m] \sim \ln^m N$$

- Transforming $\alpha_s^n \ln^m N$ -terms up to N³LO for unpolarized TMDPDF and TMDFF

$$\lim_{N \rightarrow \infty} \mathbf{M}_N[C_{ij}^{f_1}] = \delta_{ij} \exp[2D_i(b_T) \ln \bar{N} + E_i(b_T)]$$

Exponentiation!

Matching Coefficient Function in Mellin Space

- Mellin transformation

$$\mathbf{M}_N[C^F] = \int_0^1 dx x^{N-1} C^F(x, b_T)$$

- Large- x asymptotics correspond to large- N dominant terms in Mellin space

$$\lim_{N \rightarrow \infty} \mathbf{M}_N[H] = 0$$

$$\lim_{N \rightarrow \infty} \mathbf{M}_N[L_0] = 1$$

$$\lim_{N \rightarrow \infty} \mathbf{M}_N[L_m] \sim \ln^m N$$

- Transforming $\alpha_s^n \ln^m N$ -terms up to N³LO for unpolarized TMDPDF and TMDFF

$$\lim_{N \rightarrow \infty} \mathbf{M}_N[C_{ij}^{f_1}] = \delta_{ij} \exp[2D_i(b_T) \ln \bar{N} + E_i(b_T)]$$

Exponentiation!

Perturbative
Collins-Soper Kernel

Renormalized
Soft Function

Resummed Matching Coefficient Function

- General to all orders and for all pure twist-2 matchings

Collinear-Soft
Function

Joint Resummation
(2211.08341)

$$\lim_{N \rightarrow \infty} \mathbf{M}_N[C_{ij}^F] = \delta_{ij} \exp[2D_i(b_T) \ln \bar{N} + E_i(b_T)] = \delta_{ij} S_i^c(b_T)$$

- At large- N , C_{ij}^F dominated by soft-gluon radiation

Resummed Matching Coefficient Function

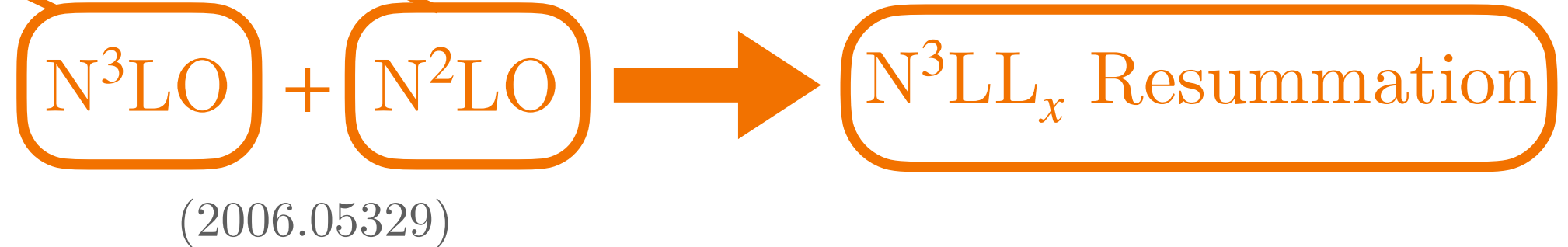
- General to all orders and for all pure twist-2 matchings

$$\lim_{N \rightarrow \infty} \mathbf{M}_N[C_{ij}^F] = \delta_{ij} \exp[2D_i(b_T) \ln \bar{N} + E_i(b_T)] = \delta_{ij} S_i^c(b_T)$$

Collinear-Soft
Function

Joint Resummation
(2211.08341)

- At large- N , C_{ij}^F dominated by soft-gluon radiation



Resummed Matching Coefficient Function

- General to all orders and for all pure twist-2 matchings

Collinear-Soft
Function

Joint Resummation
(2211.08341)

$$\lim_{N \rightarrow \infty} \mathbf{M}_N[C_{ij}^F] = \delta_{ij} \exp[2D_i(b_T) \ln \bar{N} + E_i(b_T)] = \delta_{ij} S_i^c(b_T)$$

- At large- N , C_{ij}^F dominated by soft-gluon radiation

N³LO

+ N²LO

(2006.05329)

N³LL_x Resummation

- Transforming back to x -space

$$C_{ij}^F(x, b_T) = \delta_{ij} \left[\delta(1-x) - \frac{2D_i(b_T)}{(1-x)_+^{1+2D_i(b_T)}} \right] \exp \left[E_i(b_T) - \sum_{k=2}^{\infty} \frac{\zeta_k}{k} (2D_i(b_T))^k \right] + \Delta C_{ij}^F(x, b_T)$$

No $L_m(x)$ -terms

$V_i(x, b_T)$

(Unpolarized Beam Function Matching - 1909.00811)

Wandzura-Wilczek Contribution

- Matching for Worm-gear distributions mix twist-2 and twist-3 PDFs

$$g_{1T}^{\perp,i}(x, b_T) = C_{ij}^{g_{1T}^{\perp}}(x, b_T) \otimes g_1^j(x) + \sum_t C_{t,ij}^{g_{1T}^{\perp}}(x, x_1, x_2, x_3, b_T) \otimes t_j(x_1, x_2, x_3) + \mathcal{O}(b_T^2)$$

$$h_{1L}^{\perp,i}(x, b_T) = C_{ij}^{h_{1L}^{\perp}}(x, b_T) \otimes h_1^j(x) + \sum_t C_{t,ij}^{h_{1L}^{\perp}}(x, x_1, x_2, x_3, b_T) \otimes \bar{t}_j(x_1, x_2, x_3) + \mathcal{O}(b_T^2)$$

Wandzura-Wilczek (WW)

- At tree-level:

$$g_{1T}^{\perp, \text{WW-tree}}(x, b_T) = x \int_x^1 \frac{dy}{y} g_1(y)$$

$$h_{1L}^{\perp, \text{WW-tree}}(x, b_T) = -x^2 \int_x^1 \frac{dy}{y^2} h_1(y)$$

Resummed Wandzura-Wilczek Contribution

- Same large- x asymptotic behavior as the leading contribution

$$F_i^{WW}(x, b_T) = \int_x^1 \frac{dy}{y} \left[V_i(y, b) F_i^{WW\text{-tree}}\left(\frac{x}{y}, b_T\right) + \sum_j \Delta C_{ij}^{WW}(y, b_T) f_j\left(\frac{x}{y}\right) \right]$$

Resummed Wandzura-Wilczek Contribution

- Same large- x asymptotic behavior as the leading contribution

$$F_i^{WW}(x, b_T) = \int_x^1 \frac{dy}{y} \left[V_i(y, b) F_i^{WW\text{-tree}}\left(\frac{x}{y}, b_T\right) + \sum_j \Delta C_{ij}^{WW}(y, b_T) f_j\left(\frac{x}{y}\right) \right]$$

- After performing tree-level integral $V_i^{WW}(x, b_T)$ (Universal Resummation term for WW terms)

$$C_{ij}^{WW}(x, b_T) = \frac{\delta_{ij}}{(1-x)^{2D_i(b_T)}} \exp \left[\overbrace{E_i(b_T) - \sum_{k=2}^{\infty} \frac{\zeta_k}{k} (2D_i(b_T))^k}^{V_i^{WW}(x, b_T)} \right] + \Delta C_{ij}^{WW}(x, b_T)$$

Resummed Wandzura-Wilczek Contribution

- Same large- x asymptotic behavior as the leading contribution

$$F_i^{WW}(x, b_T) = \int_x^1 \frac{dy}{y} \left[V_i(y, b) F_i^{WW\text{-tree}}\left(\frac{x}{y}, b_T\right) + \sum_j \Delta C_{ij}^{WW}(y, b_T) f_j\left(\frac{x}{y}\right) \right]$$

- After performing tree-level integral $V_i^{WW}(x, b_T)$ (Universal Resummation term for WW terms)

$$C_{ij}^{WW}(x, b_T) = \frac{\delta_{ij}}{(1-x)^{2D_i(b_T)}} \exp \left[\overbrace{E_i(b_T) - \sum_{k=2}^{\infty} \frac{\zeta_k}{k} (2D_i(b_T))^k}^{V_i^{WW}(x, b_T)} \right] + \Delta C_{ij}^{WW}(x, b_T)$$

- NLO remainder terms vanish as $x \rightarrow 1$: $\Delta C_{qq}^{g_{1T}^\perp}(x, b_T) = 2a_s C_F (\mathbf{L}_\mu - 1) (\ln(x) + (1-x)) + \mathcal{O}(a_s^2)$

$$\Delta C_{qq}^{h_{1L}^\perp}(x, b_T) = 4a_s C_F \mathbf{L}_\mu \ln(x) + \mathcal{O}(a_s^2)$$

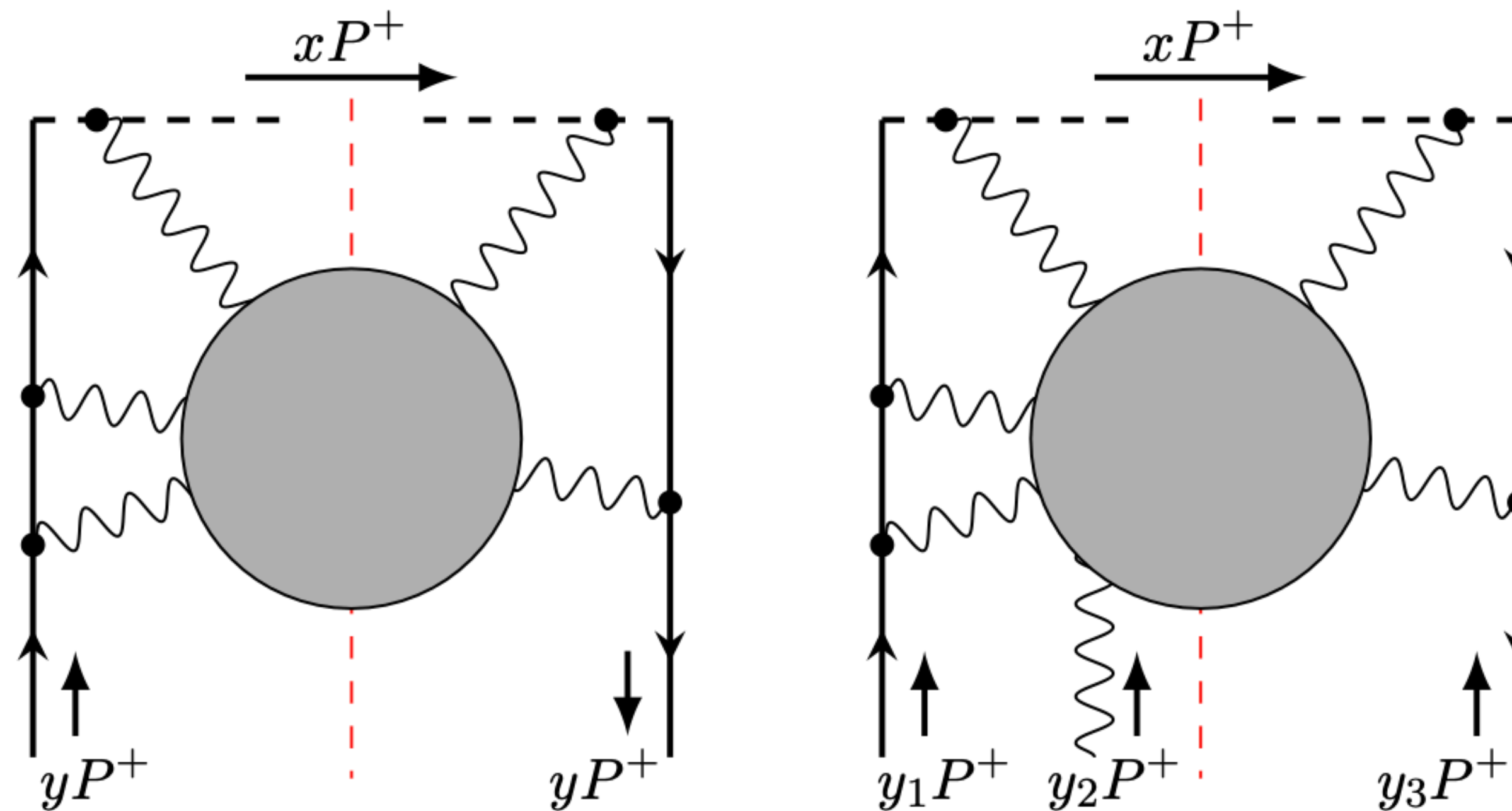
LL_x and NLL_x successfully resummed!

Twist-3 Contributions

$$F_i(x, b_T) = C_{ij}^F(x, b_T) \otimes f_j(x) + \sum_t C_{t,ij}^F(x, x_1, x_2, x_3, b_T) \otimes t_j(x_1, x_2, x_3) + \mathcal{O}(b_T^2)$$

Twist-3 Matching

- For twist-3 matching, only resummation to LL_x



Resummed Twist-3 Contributions

- Sivers and Boer-Mulders are simplest

$$f_{1T,q}^\perp(x, b_T) = \pm \frac{\pi e^{a_s E_q^{(1)}(b_T)}}{(1-x)^{2a_s D_q^{(1)}(b_T)}} T_q(-x, 0, x) + \sum_t \Delta C_{t,ij}^{f_{1T}^\perp}(x, x_1, x_2, x_3, b_T) \otimes \hat{t}_j(x_1, x_2, x_3) + \mathcal{O}(b_T^2)$$

$$h_{1,q}^\perp(x, b_T) = \mp \frac{\pi e^{a_s E_q^{(1)}(b_T)}}{(1-x)^{2a_s D_q^{(1)}(b_T)}} E_q(-x, 0, x) + \sum_t \Delta C_{t,ij}^{h_1^\perp}(x, x_1, x_2, x_3, b_T) \otimes \tilde{t}_j(x_1, x_2, x_3) + \mathcal{O}(b_T^2)$$

Resummed Twist-3 Contributions

- Sivers and Boer-Mulders are simplest

$$\begin{aligned}
 f_{1T,q}^\perp(x, b_T) &= \pm \frac{\pi e^{a_s E_q^{(1)}(b_T)}}{(1-x)^{2a_s D_q^{(1)}(b_T)}} T_q(-x, 0, x) + \sum_t \Delta C_{t,ij}^{f_{1T}^\perp}(x, x_1, x_2, x_3, b_T) \otimes \hat{t}_j(x_1, x_2, x_3) + \mathcal{O}(b_T^2) \\
 h_{1,q}^\perp(x, b_T) &= \mp \frac{\pi e^{a_s E_q^{(1)}(b_T)}}{(1-x)^{2a_s D_q^{(1)}(b_T)}} E_q(-x, 0, x) + \sum_t \Delta C_{t,ij}^{h_1^\perp}(x, x_1, x_2, x_3, b_T) \otimes \tilde{t}_j(x_1, x_2, x_3) + \mathcal{O}(b_T^2) \\
 &\quad \text{LL}_x + \text{some NLL}_x
 \end{aligned}$$

Resummed Twist-3 Contributions

- Sivers and Boer-Mulders are simplest

$$f_{1T,q}^\perp(x, b_T) = \pm \frac{\pi e^{a_s E_q^{(1)}(b_T)}}{(1-x)^{2a_s D_q^{(1)}(b_T)}} T_q(-x, 0, x) + \sum_t \Delta C_{t,ij}^{f_{1T}^\perp}(x, x_1, x_2, x_3, b_T) \otimes \hat{t}_j(x_1, x_2, x_3) + \mathcal{O}(b_T^2)$$

$$h_{1,q}^\perp(x, b_T) = \mp \frac{\pi e^{a_s E_q^{(1)}(b_T)}}{(1-x)^{2a_s D_q^{(1)}(b_T)}} E_q(-x, 0, x) + \sum_t \Delta C_{t,ij}^{h_1^\perp}(x, x_1, x_2, x_3, b_T) \otimes \tilde{t}_j(x_1, x_2, x_3) + \mathcal{O}(b_T^2)$$

LL_x + some NLL_x

- Reminder terms do not vanish in the large- x limit \longrightarrow Subleading NLL_x contributions

$$[\Delta C_{T,qq}^{f_{1T}^\perp} \otimes T_q](x, b_T) = a_s \left(2\mathbf{L}_\mu \left(2C_F - \frac{C_A}{2} \right) T_q(-x, 0, x) + \dots \right)$$

$$[\Delta C_{E,qq}^{h_1^\perp} \otimes E_q](x, b_T) = a_s \left(-2\mathbf{L}_\mu \left(\frac{3C_F}{2} - \frac{C_A}{2} \right) E_q(-x, 0, x) + \dots \right)$$

Large- x Resummation Implications

- Phenomenological fitting ansatz for TMDs

$$F_i(x, b_T) = C_{ij}^F(x, b^*(b_T); \mu_{OPE}) \otimes f_j(x; \mu_{OPE}) \cdot f_{NP}(x, b_T)$$

Non-perturbative
models

- Resummation at large- x restricts our models

$$2D_i(b^*(b_T); \mu_{OPE}) < 1$$

Large- x Resummation Implications

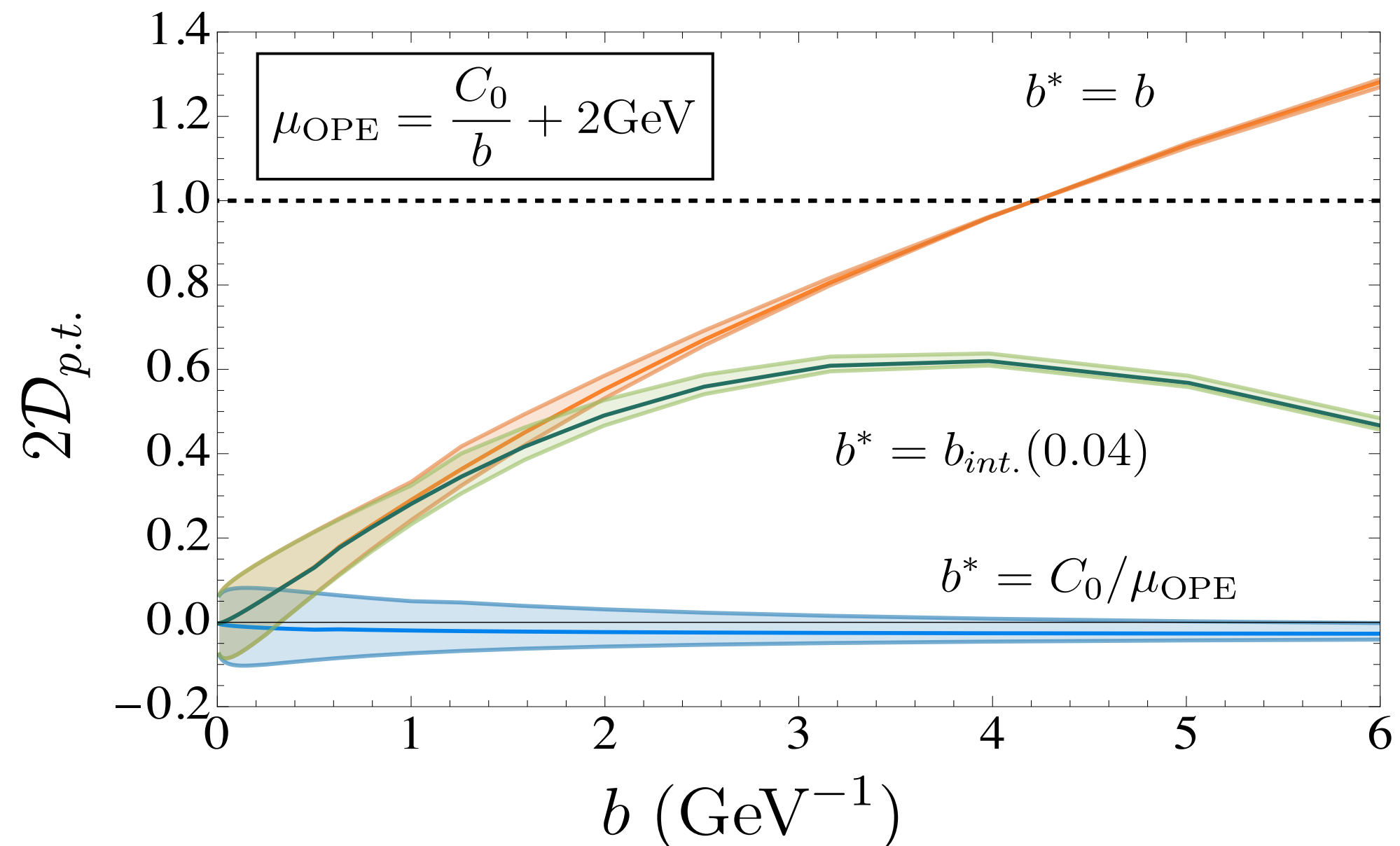
- Phenomenological fitting ansatz for TMDs

$$F_i(x, b_T) = C_{ij}^F(x, b^*(b_T); \mu_{OPE}) \otimes f_j(x; \mu_{OPE}) \cdot f_{NP}(x, b_T)$$

Non-perturbative models

- Resummation at large- x restricts our models

$$2D_i(b^*(b_T); \mu_{OPE}) < 1$$



- ART23 linear b^* -model breaks this constraint

(ART23: 2305.07473)

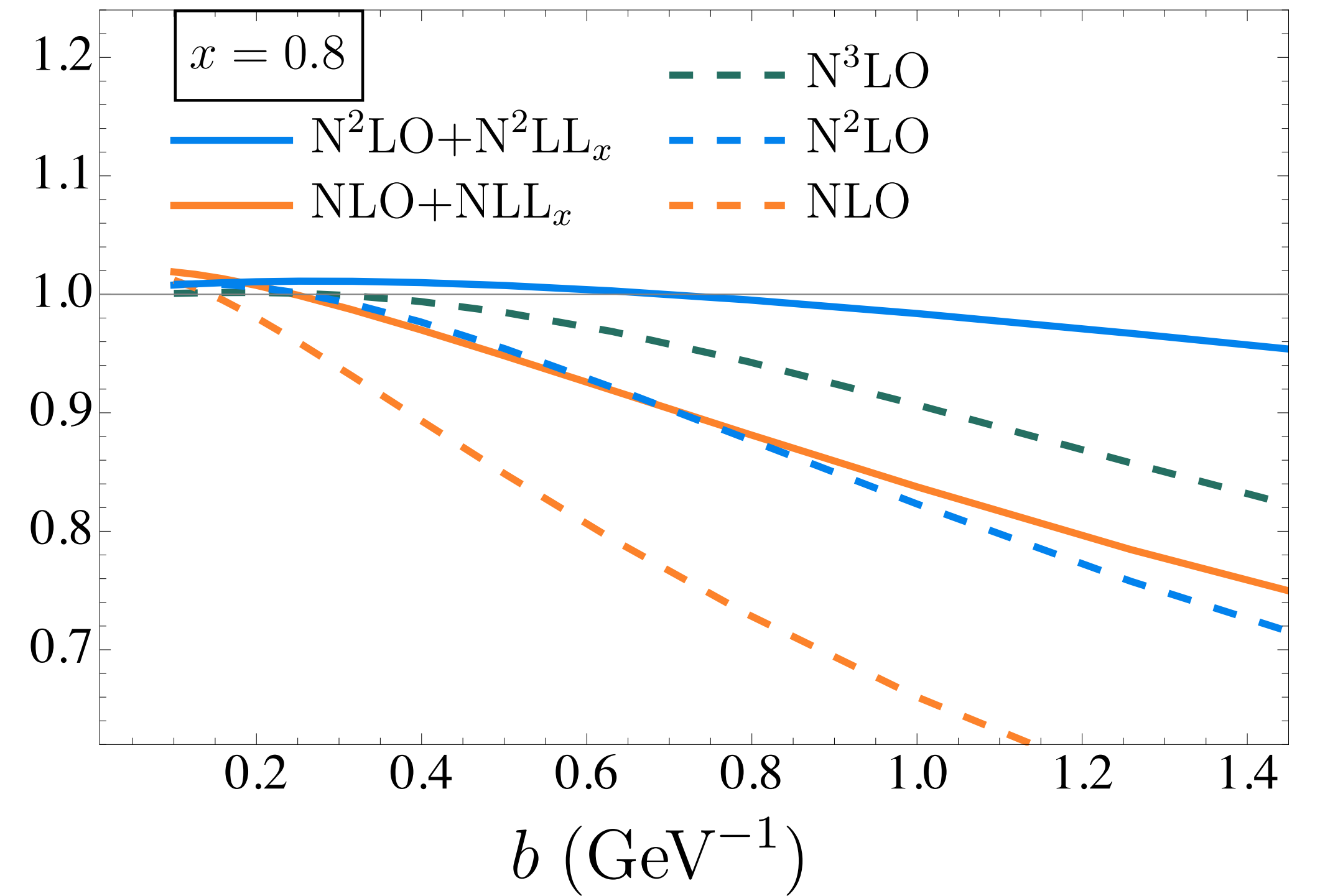
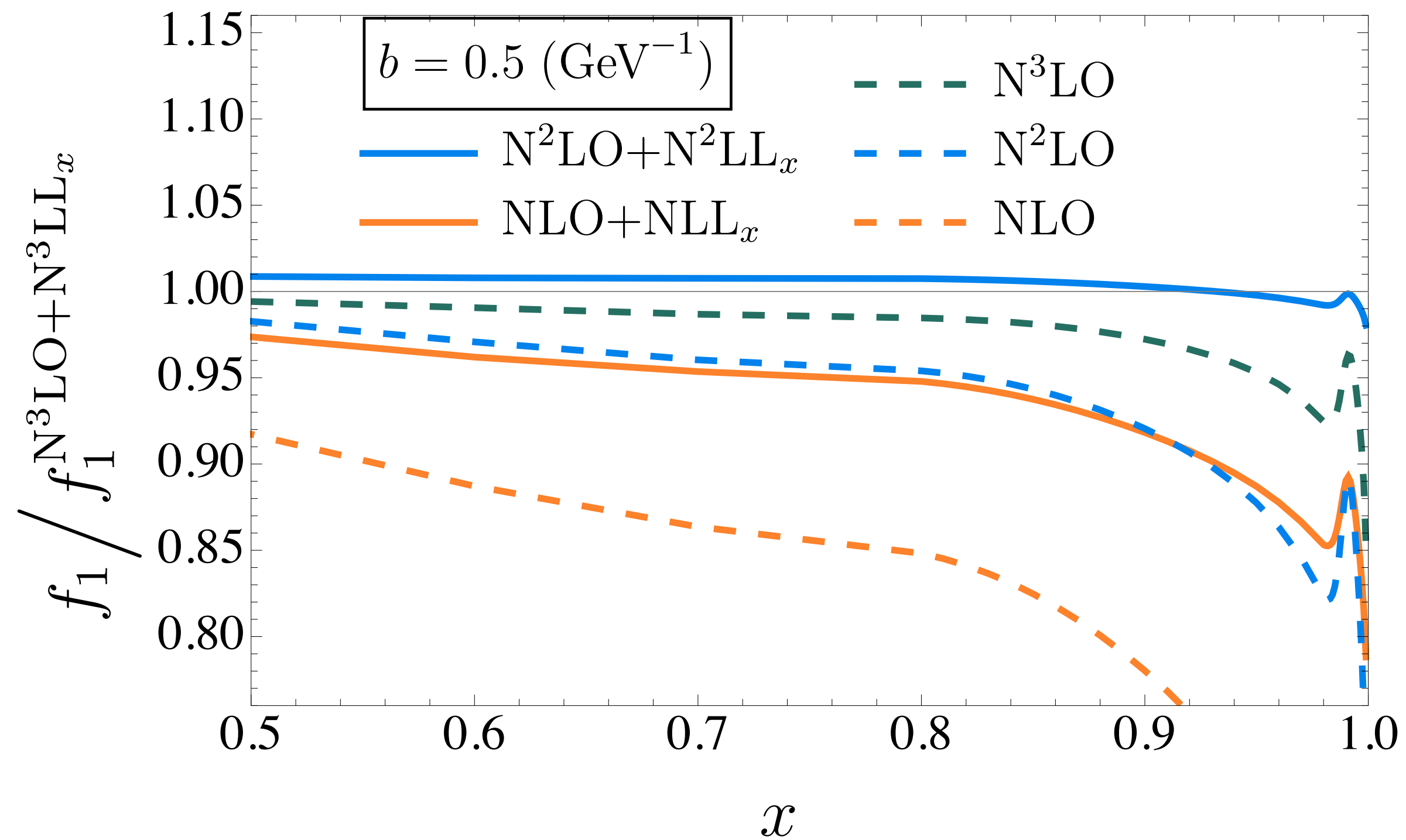
- In ART25 resummation is used with new model:

$$b_{int.}^*(a, b) = be^{-ab^2} + \frac{2e^{-\gamma_E}}{\mu_{OPE}(b)} \left(1 - e^{-ab^2}\right)$$

(ART25: 2503.11201)

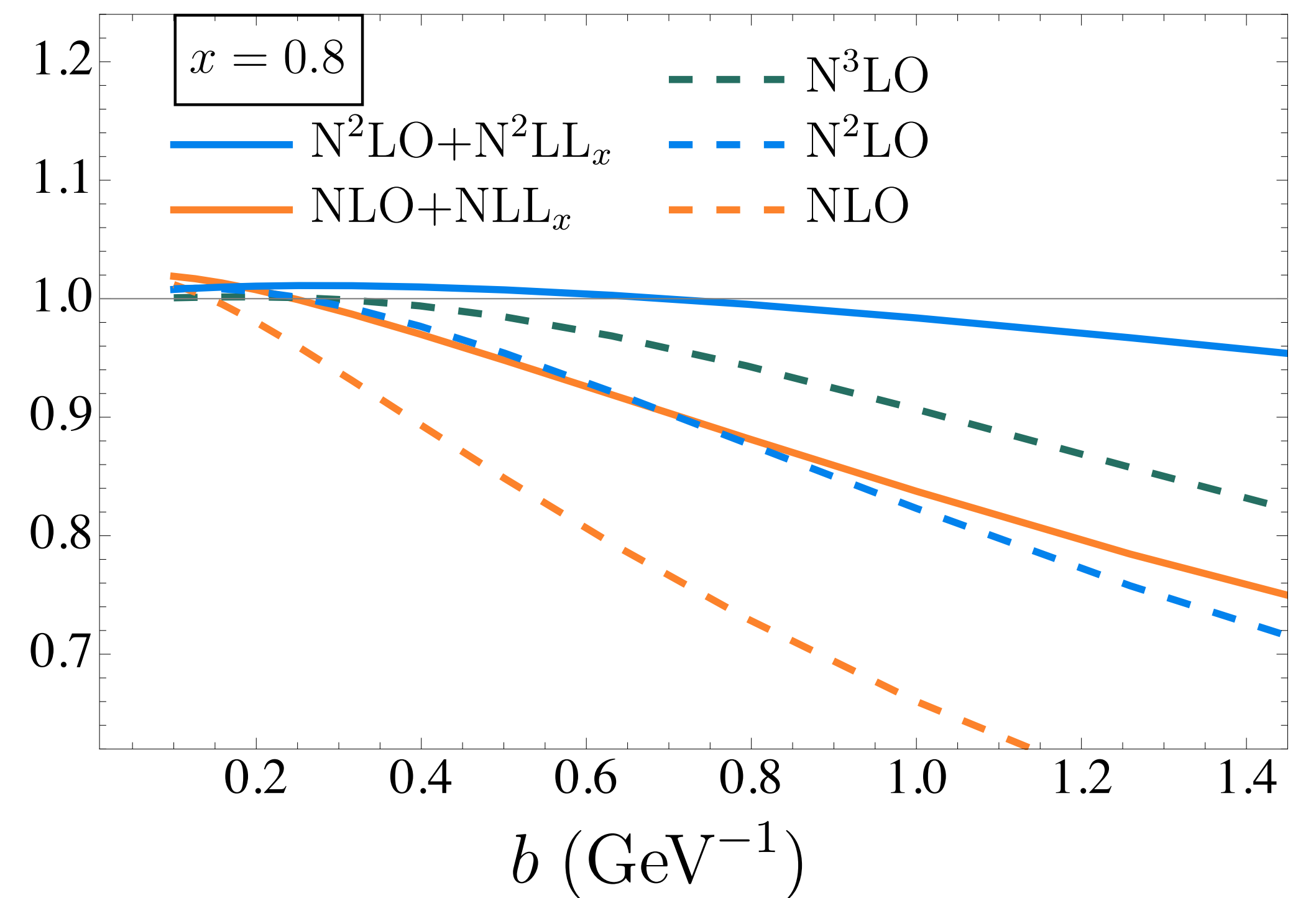
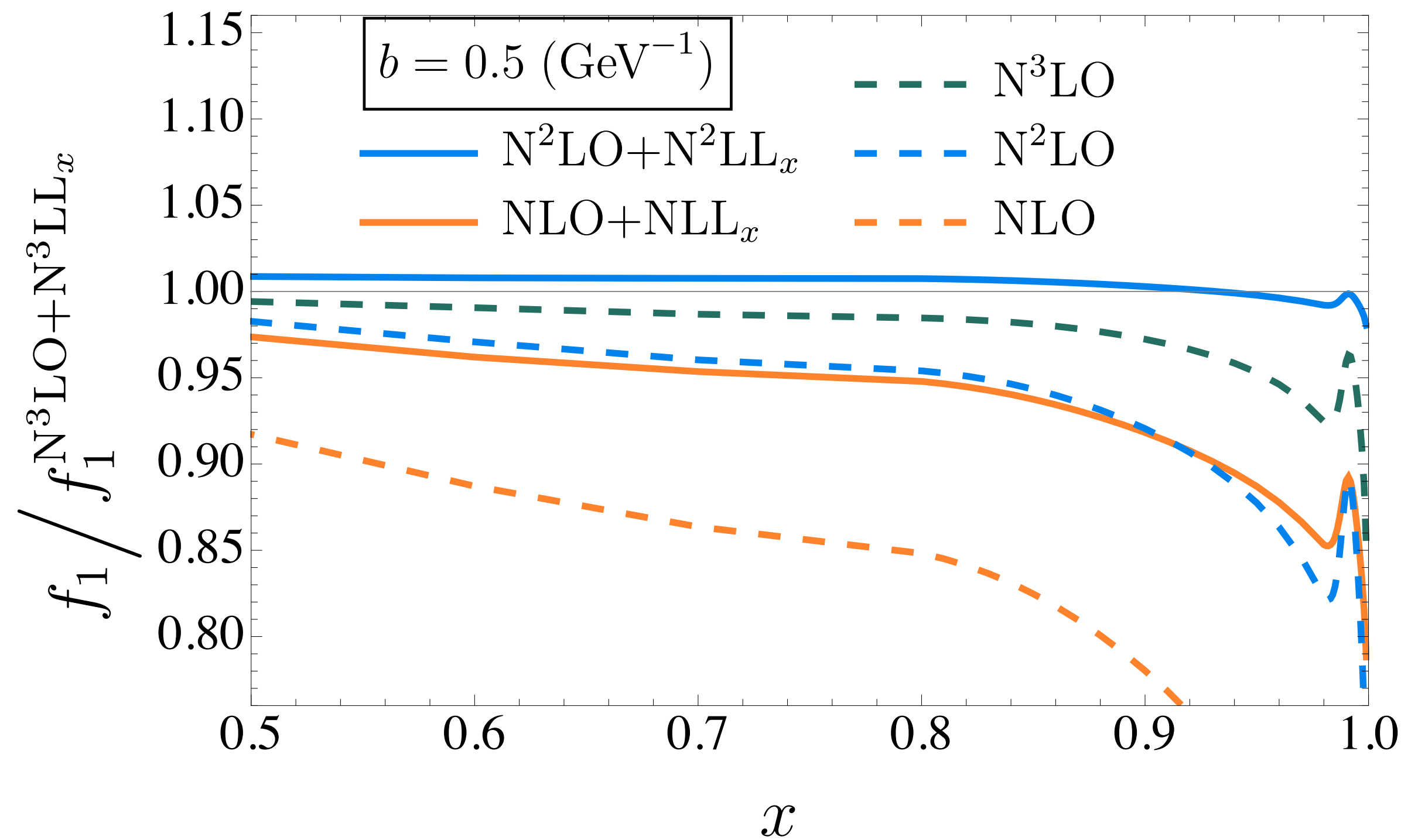
Large- x Resummation Impact

- Unpolarized TMDPDF (u-quark)



Large- x Resummation Impact

- Unpolarized TMDPDF (u-quark)



Large- x Resummation

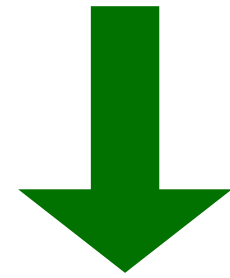
Bigger differences for $x \gtrsim 0.5$ and $b_T \gtrsim 0.3 \text{ GeV}^{-1}$

Faster convergence (approximate higher orders)

Large- x Resummation Impact

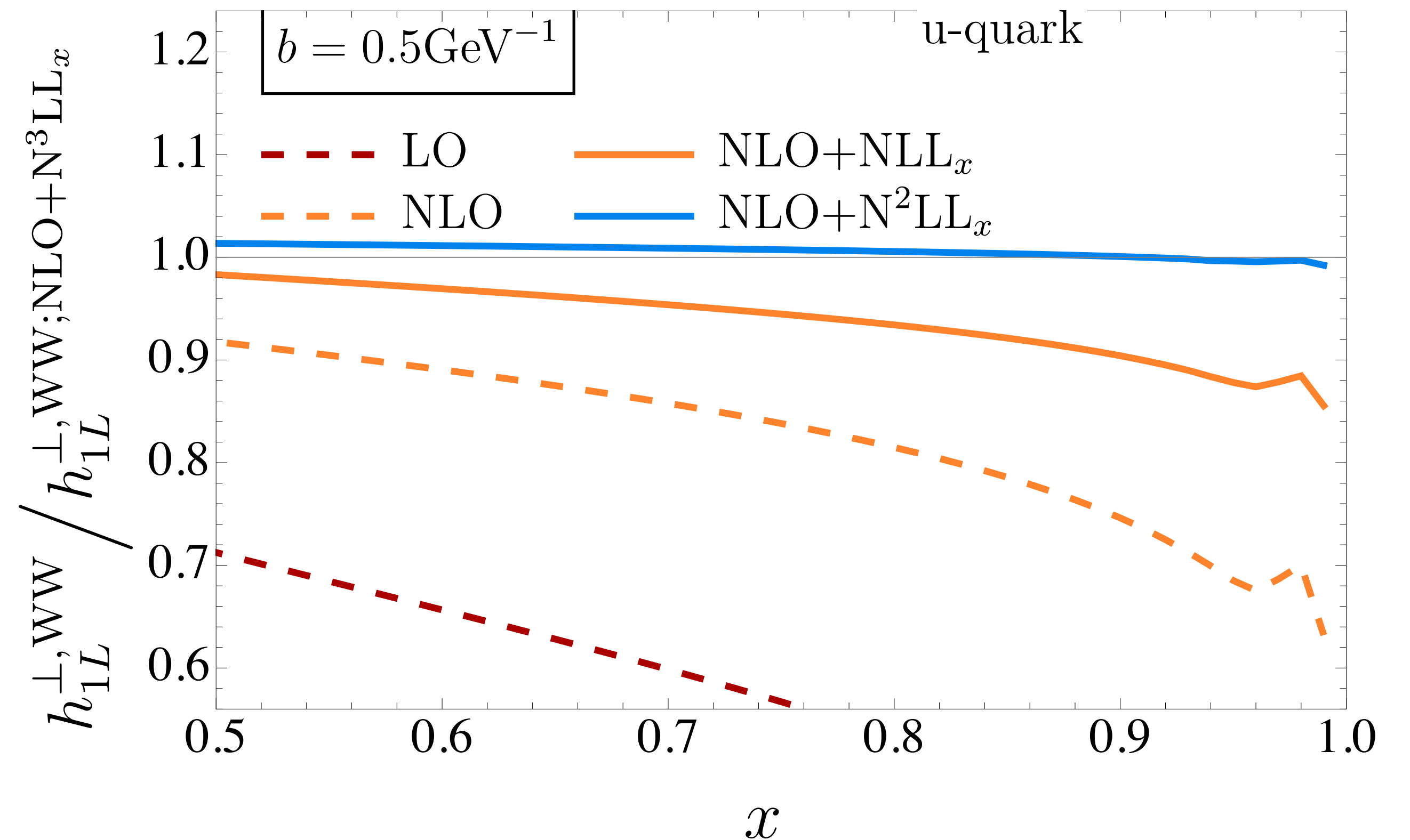
- WW-contribution to Worm-gear-L

Only NLO coefficient available



Greater impact of N^3LL_x resummation

(Similarly for helicity and Worm-gear-T distributions)



Conclusions

- Large- x resummation directly within TMDs
 - ▶ Process-independent and universal
 - ▶ Valid for all leading TMDPDFs (except for pretzelosity) and TMDFFs
- First results for large- x asymptotics of higher twist matchings
 - ▶ Wandzura-Wilczek contribution valid to all log-orders
 - ▶ Twist-3 contribution valid to LL_x
- Resummation significantly improves extraction of many TMDs

Thank you for your attention!



PID2022-136510NB-C31



U N I V E R S I D A D
COMPLUTENSE
M A D R I D



Óscar del Río. Complutense University of Madrid