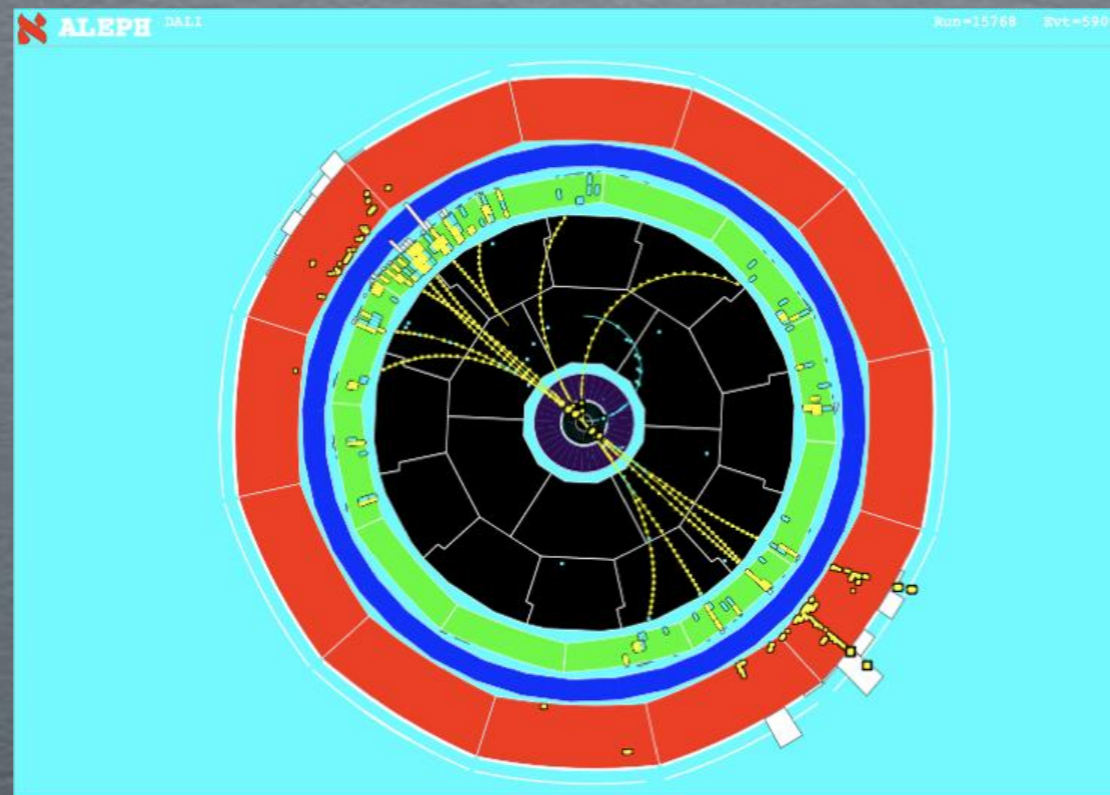


COHERENCE VIOLATION IN JET OBSERVABLES



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IN COLLABORATION WITH J. HOLGUIN AND J. FORSHAW
QCD EVOLUTION 2026 – MADRID – 14 MAY 2026

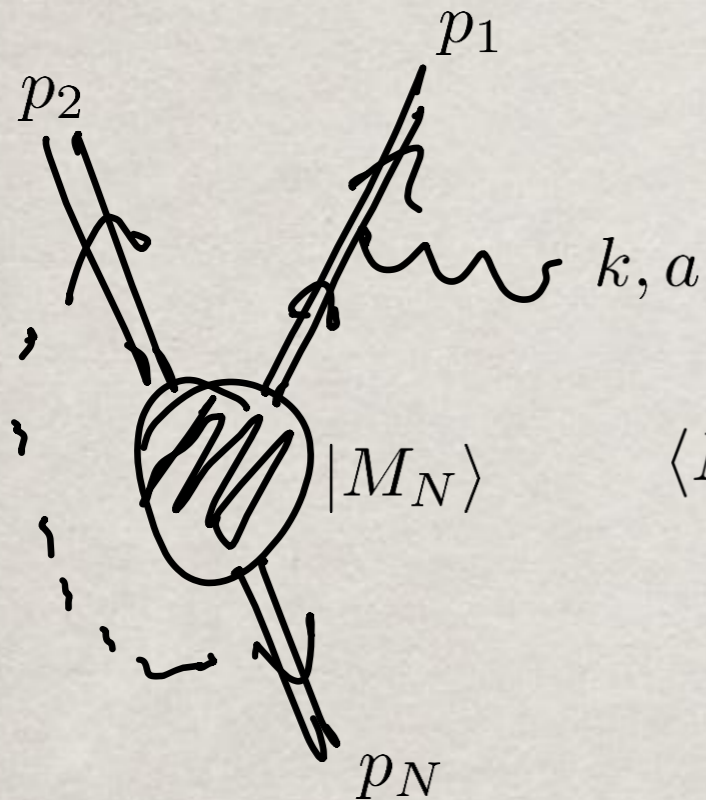
OUTLINE

- What is coherence of QCD radiation?
- Super-leading logarithms in gaps between jets
- Super-super-leading logarithms in one-jettiness

WHAT IS COHERENCE?

SOFT AMPLITUDE SQUARED

It is useful to introduce a representation-independent notation for soft radiation



$$\underbrace{|M(p_1, \dots, p_N, k)\rangle}_{\equiv |M_{N+1}\rangle} = \sum_{i=1}^N \mathbf{T}_i \frac{p_i \cdot \varepsilon(k)}{p_i \cdot k} \underbrace{|M(p_1, \dots, p_N)\rangle}_{\equiv |M_N\rangle}$$

$$\langle M_{N+1} | M_{N+1} \rangle = - \sum_{i=1}^N \sum_{j \neq i}^N \frac{p_i \cdot p_j}{(p_i \cdot k)(p_j \cdot k)} \langle M_N | \mathbf{T}_i \cdot \mathbf{T}_j | M_N \rangle$$

$$\mathbf{T}_i \cdot \mathbf{T}_j \equiv \sum_a \mathbf{T}_i^a \mathbf{T}_j^a$$

The amplitude squared can be also written in terms of a colour-density matrix

$$\langle M_{N+1} | M_{N+1} \rangle = - \sum_{i=1}^N \sum_{j \neq i}^N \frac{p_i \cdot p_j}{(p_i \cdot k)(p_j \cdot k)} \text{Tr} [(\mathbf{T}_i \cdot \mathbf{T}_j) \mathbf{H}_N]$$

$$\mathbf{H}_N \equiv |M_N\rangle \langle M_N|$$

$$\text{Tr}(\mathbf{H}_N) = \mathcal{M}_N^2$$

COLOUR CONSERVATION

Colour conservation can be used to further simplify the square amplitude

$$\langle M_{N+1} | M_{N+1} \rangle = - \sum_{i=1}^N \sum_{j \neq i} \frac{p_i \cdot p_j}{(p_i \cdot k)(p_j \cdot k)} \langle M_N | \mathbf{T}_i \cdot \mathbf{T}_j | M_N \rangle$$

- Reconstruction of Casimir once one sums over all legs

$$\mathbf{T}_1 + \mathbf{T}_2 + \cdots + \mathbf{T}_N = 0 \implies \mathbf{T}_i = - \sum_{j \neq i} \mathbf{T}_j \implies - \sum_{j \neq i} \mathbf{T}_i \cdot \mathbf{T}_j = \mathbf{T}_i^2 = C_i$$

- Simplification of colour algebra up to three hard emitters

$$\mathbf{T}_1 + \mathbf{T}_2 + \mathbf{T}_3 = 0 \implies (\mathbf{T}_i + \mathbf{T}_j)^2 = -\mathbf{T}_k^2 = -C_k \implies -\mathbf{T}_i \cdot \mathbf{T}_j = \frac{C_i + C_j - C_k}{2} \mathbf{1}$$

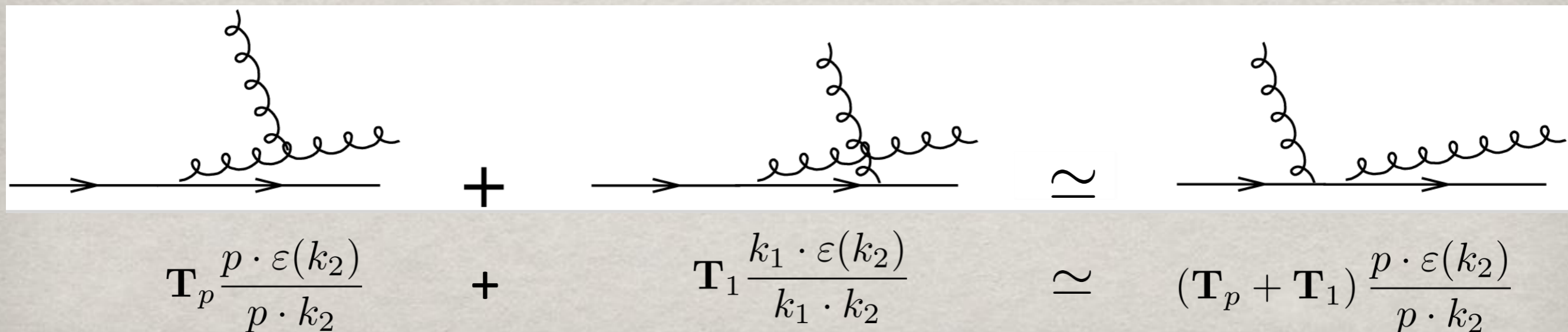
COHERENCE

All-order calculations of QCD observables rely heavily on the fact that soft emissions widely separated in angle are emitted independently off the hard legs



This property is a consequence of “coherence” of QCD radiation: gluons at large angles feel only the total colour charge of emitters

[Bassetto Ciafaloni Marchesini Phys. Rept. 100 (1983) 201]

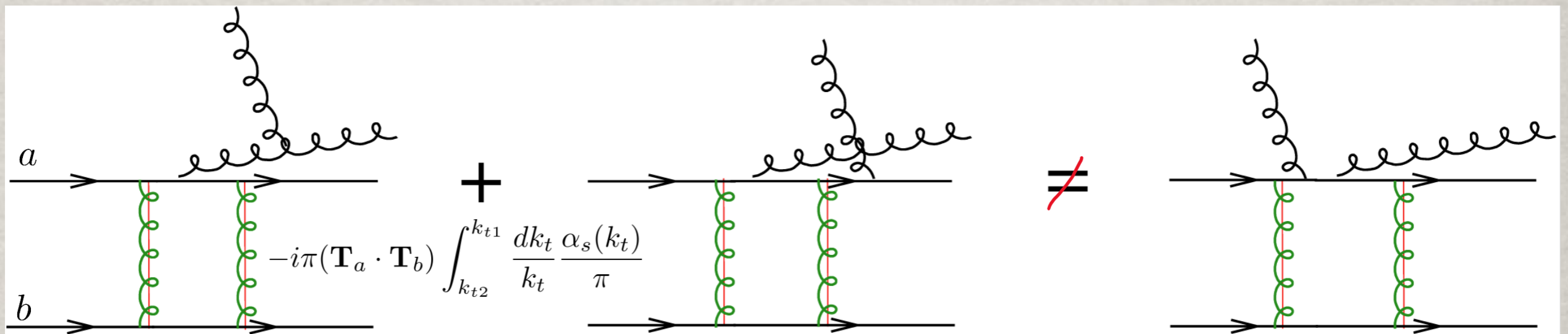


COHERENCE VIOLATING LOGARITHMS

In hadron collisions, coherence is violated in the presence of Coulomb (Glauber) gluons, which can transfer colour from one incoming parton to the other

$$S_{\mathbf{p}}^{(1)}(p_1, p_2; \tilde{P}; p_3, \dots, p_n) = S_{\mathbf{p}_H}^{(1)}(p_1, p_2; \tilde{P}) + I_C(p_1, p_2; p_3, \dots, p_n) S_{\mathbf{p}}^{(0)}(p_1, p_2; \tilde{P}),$$

[Catani De Florian Rodrigo 1112.4405] (4.2)



Coulomb-gluon exchanges (subleading in N_c)

- can endanger the factorisation of collinear singularities into parton distribution functions \Rightarrow factorisation proofs needed

[Becher Hager Jaskiewicz Neubert Schwienbacher 2408.10308]

- even in the presence of collinear factorisation, they give rise to coherence-violating logarithms (CVLs) that are not captured by “traditional” resummation techniques

[Forshaw Kyrieleis Seymour hep-ph/0604094]

SUPER-LEADING LOGARITHMS

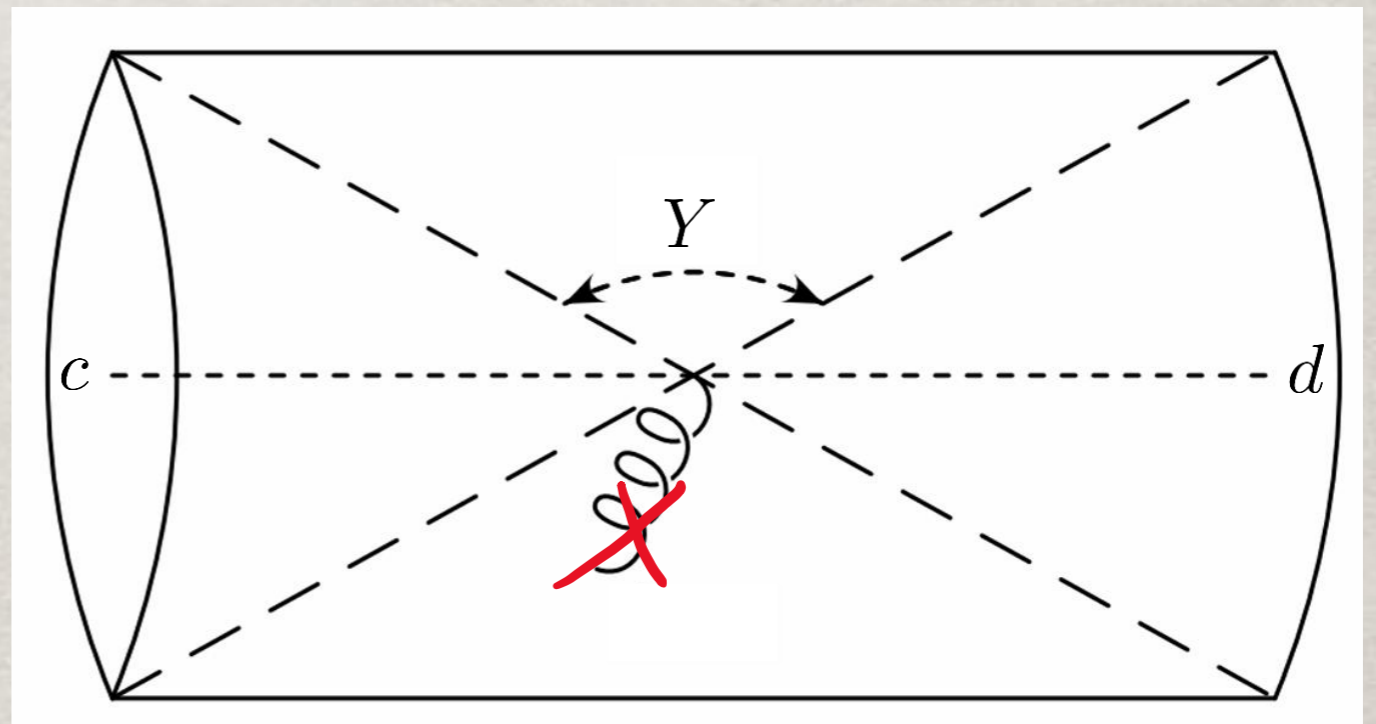
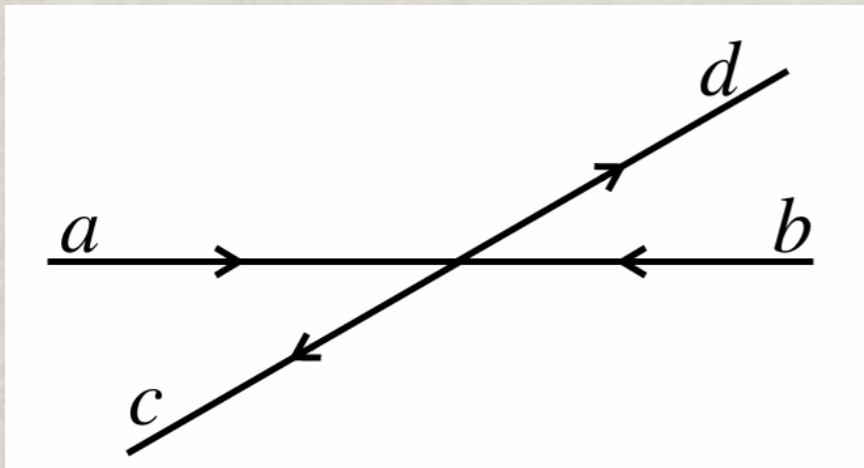
RAPIDITY GAP BETWEEN JETS

Consider the cross section for two jets with large transverse momentum $\sim Q$ and no jets with transverse momentum larger than $Q_0 \ll Q$ in a rapidity gap between the jets of width Y

$$\frac{d\sigma}{dY} \approx f_a(Q) \otimes f_b(Q) \otimes \frac{d\hat{\sigma}_{ab}}{dY} \times \Sigma(Q_0)$$

(gap) survival probability

$$\Sigma(Q_0) \approx \text{Prob} \left[\max_{i \in \text{out}} k_{Ti} < Q_0 \right]$$



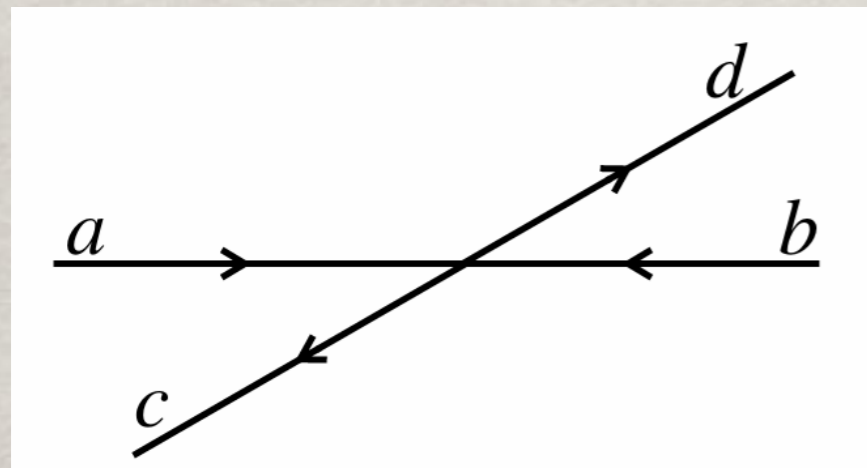
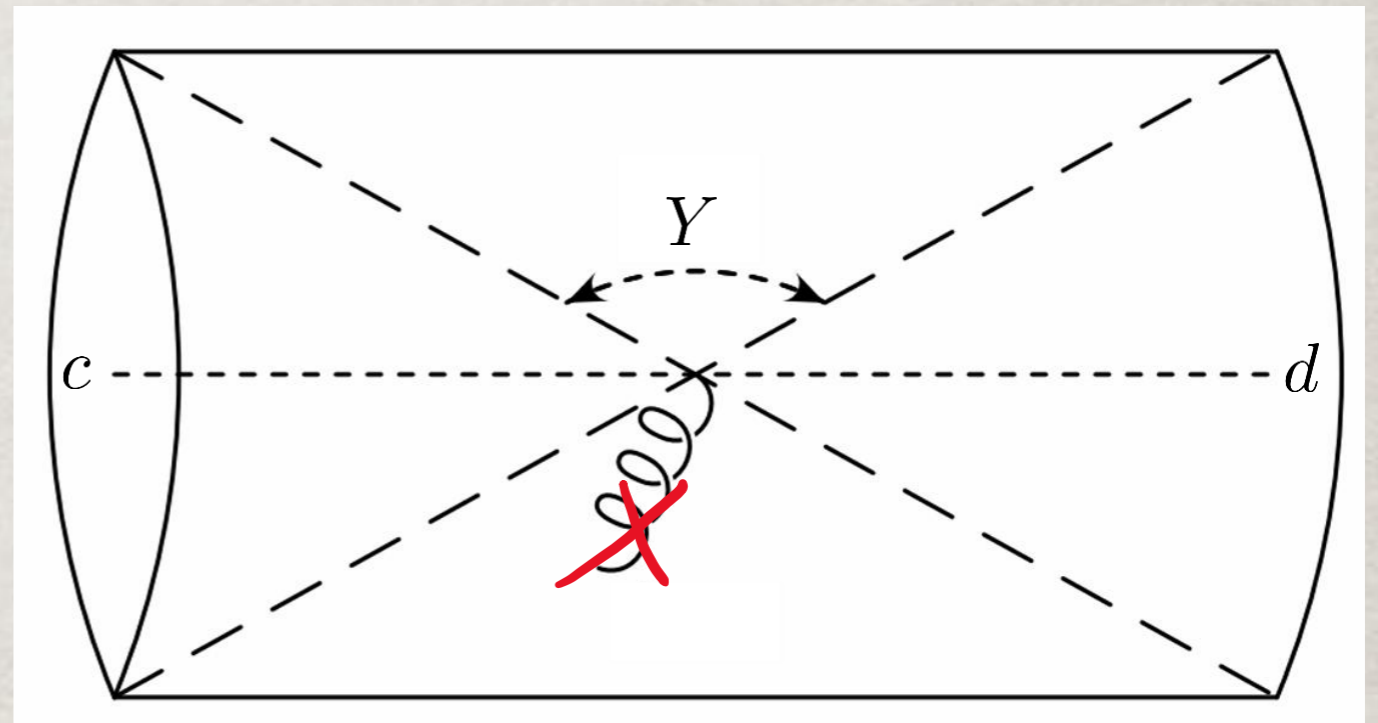
COMPUTING THE SURVIVAL PROBABILITY

The first-ever resummation of the gap survival probability vetoes all gluons emitted from the hard legs only

[Oderda Sterman hep-ph/9806530]

$$\Sigma^{\text{OS}}(Q_0) = \text{Tr} \left(\mathbf{V}_{Q_0, Q} \mathbf{H} \mathbf{V}_{Q_0, Q}^\dagger \right)$$

[Forshaw Holguin 2109.03665]



$$\mathbf{V}_{Q_0, Q} \approx \exp \left[-\frac{\alpha_s}{\pi} \ln \frac{Q}{Q_0} (Y \mathbf{T}_t^2 + i\pi \mathbf{T}_s^2) \right]$$

$$\mathbf{T}_t^2 = (\mathbf{T}_a + \mathbf{T}_c)^2 = (\mathbf{T}_b + \mathbf{T}_d)^2$$

$$\mathbf{T}_s^2 = (\mathbf{T}_a + \mathbf{T}_b)^2 = (\mathbf{T}_c + \mathbf{T}_d)^2$$

$$[\mathbf{T}_t^2, \mathbf{T}_s^2] \neq 0$$

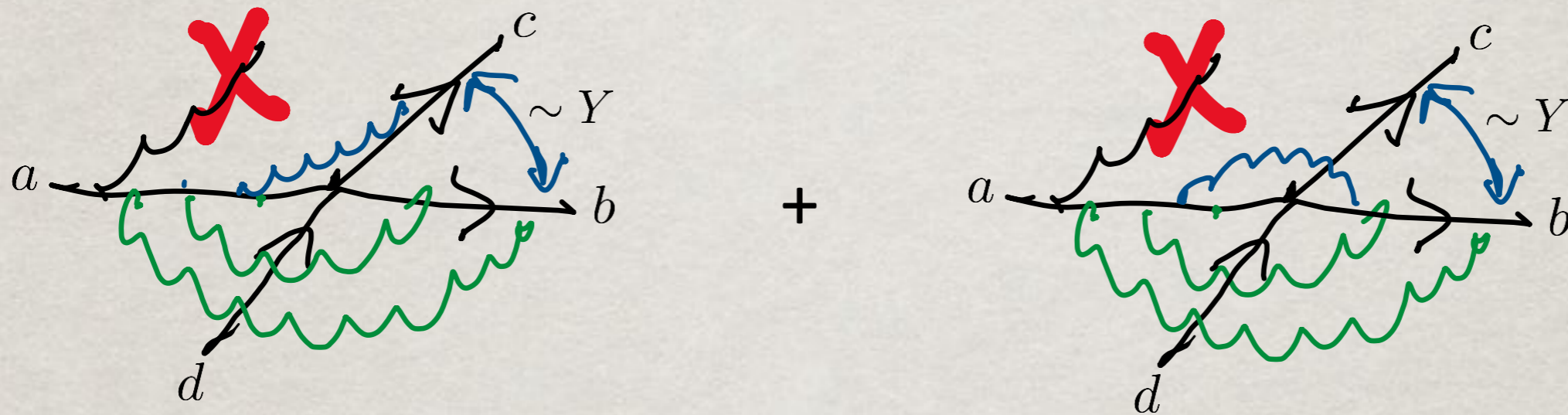
It is known that this approximation misses single-logarithmic contributions known as non-global logarithms

[Dasgupta Salam hep-ph/0104277]

SUPER-LEADING LOGARITHMS

Beyond the large- N_c limit, real emissions outside the gap can change the colour space of virtual corrections

[Forshaw Kyrieleis Seymour 0808.1269]

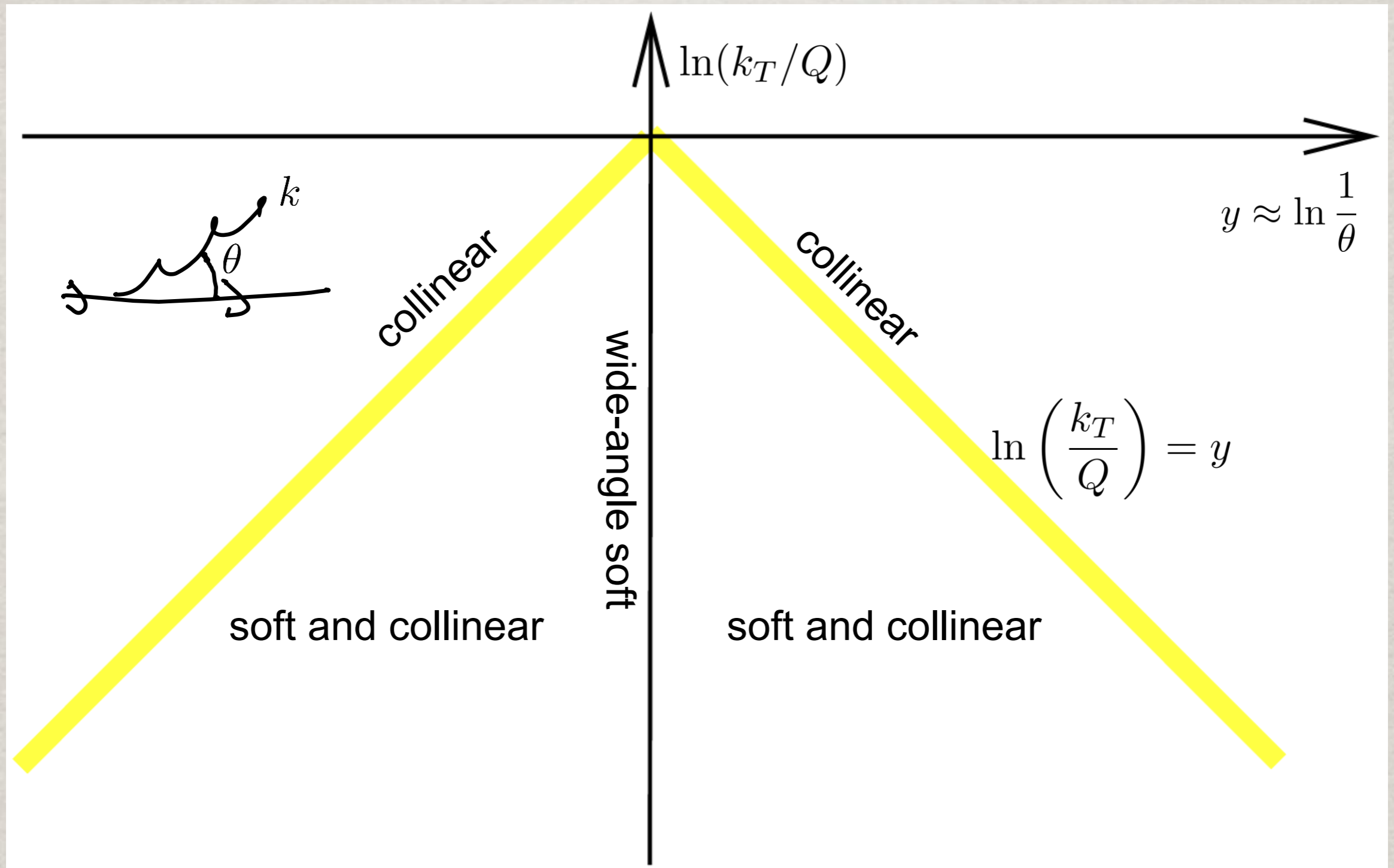


$$\begin{aligned} \Sigma^{\text{CVL}}(Q_0) &\approx \frac{\alpha_s}{\pi} \int_{Q_0}^Q \frac{dk_T}{k_T} \int_0^{\ln(Q/k_T)} dy \Theta(y - Y) \times \\ &\times \left[\text{Tr} \left(\mathbf{V}_{Q_0, k_T} \mathbf{T}_a \mathbf{V}_{k_T, Q} \mathbf{H} \mathbf{V}_{k_T, Q}^\dagger \mathbf{T}_a^\dagger \mathbf{V}_{Q_0, k_T}^\dagger \right) - C_F \text{Tr} \left(\mathbf{V}_{Q_0, Q} \mathbf{H} \mathbf{V}_{Q_0, Q}^\dagger \right) \right] \\ &\sim \frac{1}{N_c^2} \left(\frac{N_c \alpha_s}{\pi} \right)^4 Y (-i\pi)^2 \ln^5 \left(\frac{Q}{Q_0} \right) \sim \alpha_s^4 L^5 \end{aligned}$$

Such contributions are one log higher than the leading logarithms $(\alpha_s \ln(Q/Q_0))^n$, hence the name super-leading logarithms

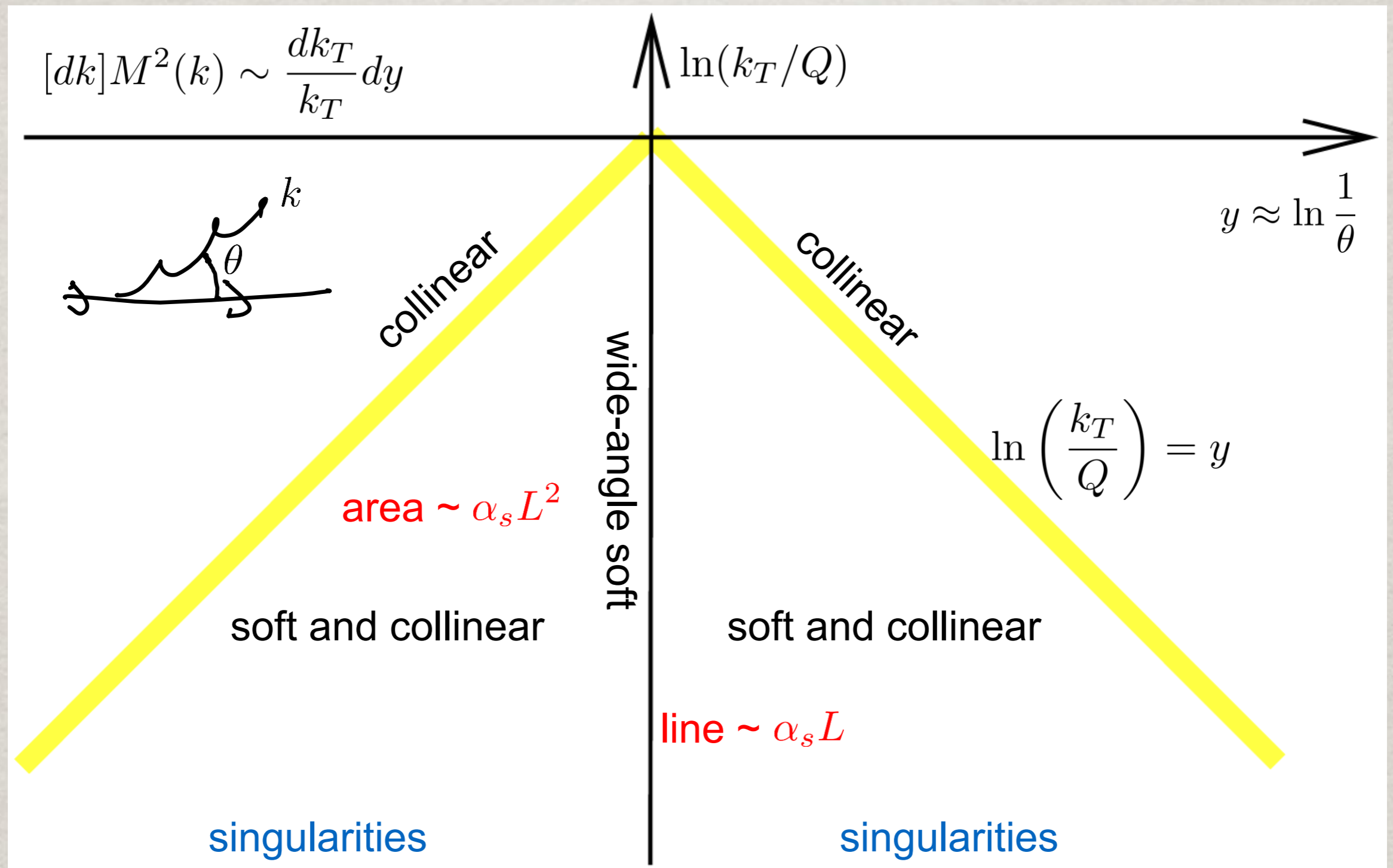
SLL IN THE LUND PLANE

The Lund plane is an effective way to picture soft/collinear emissions



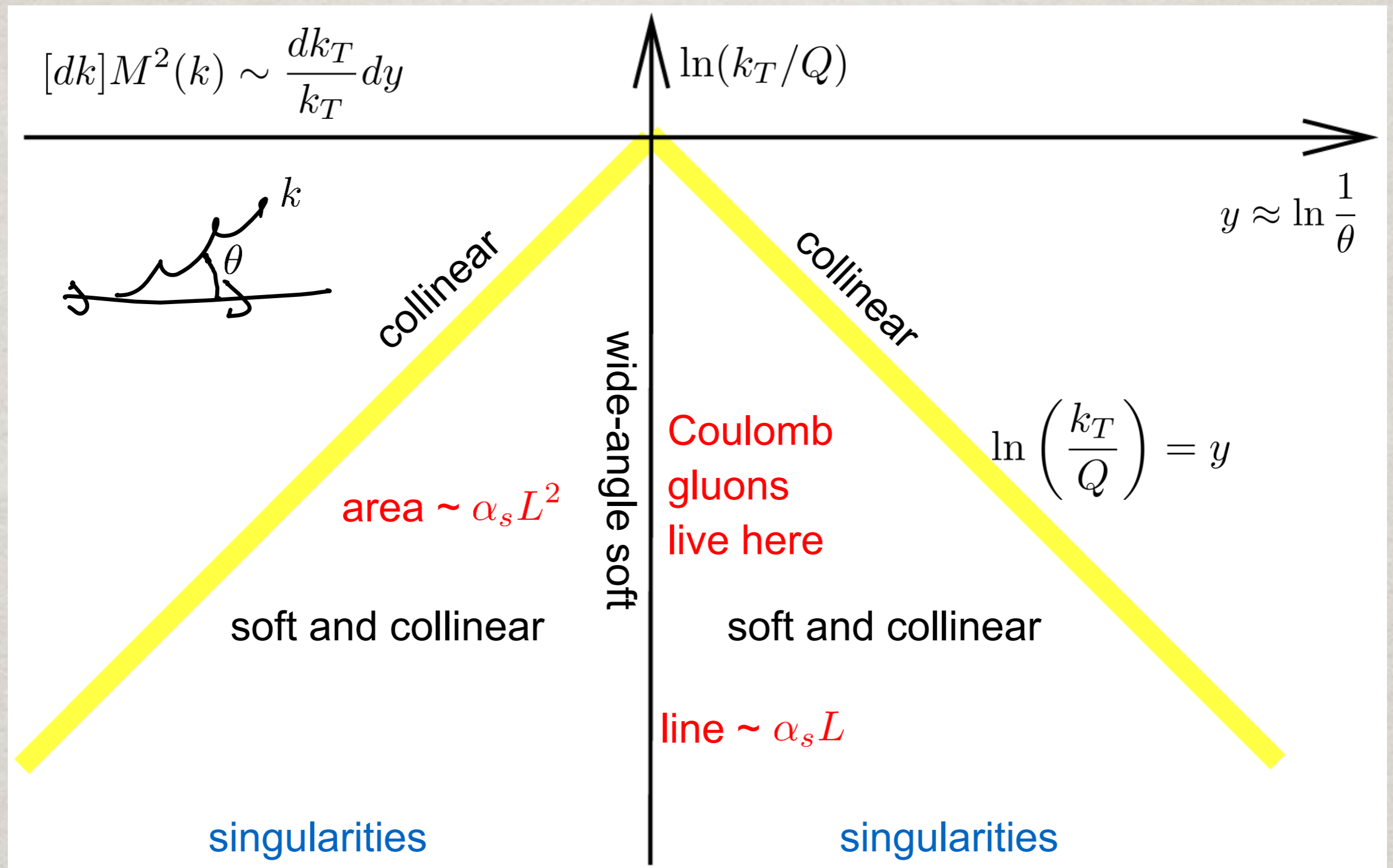
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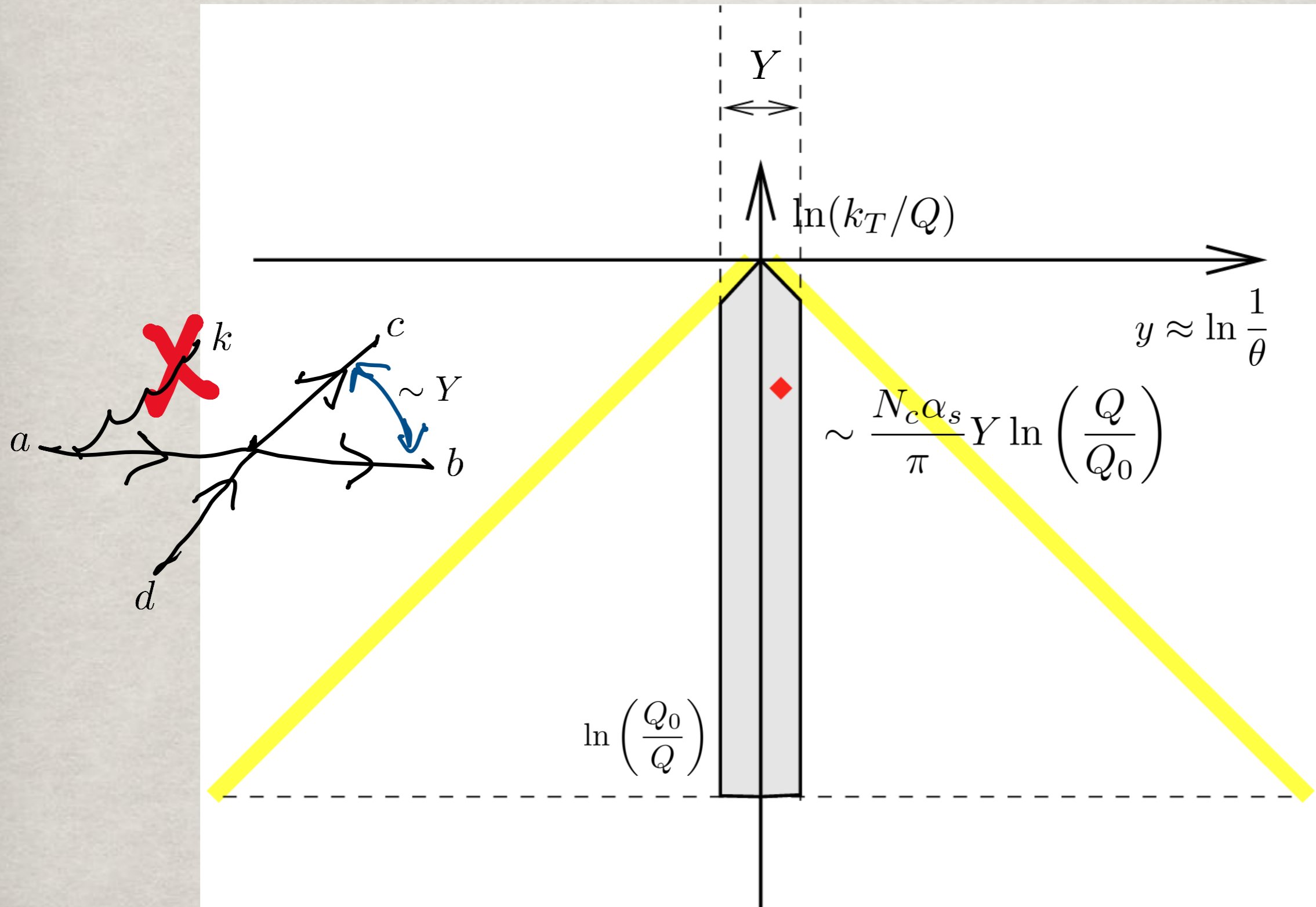
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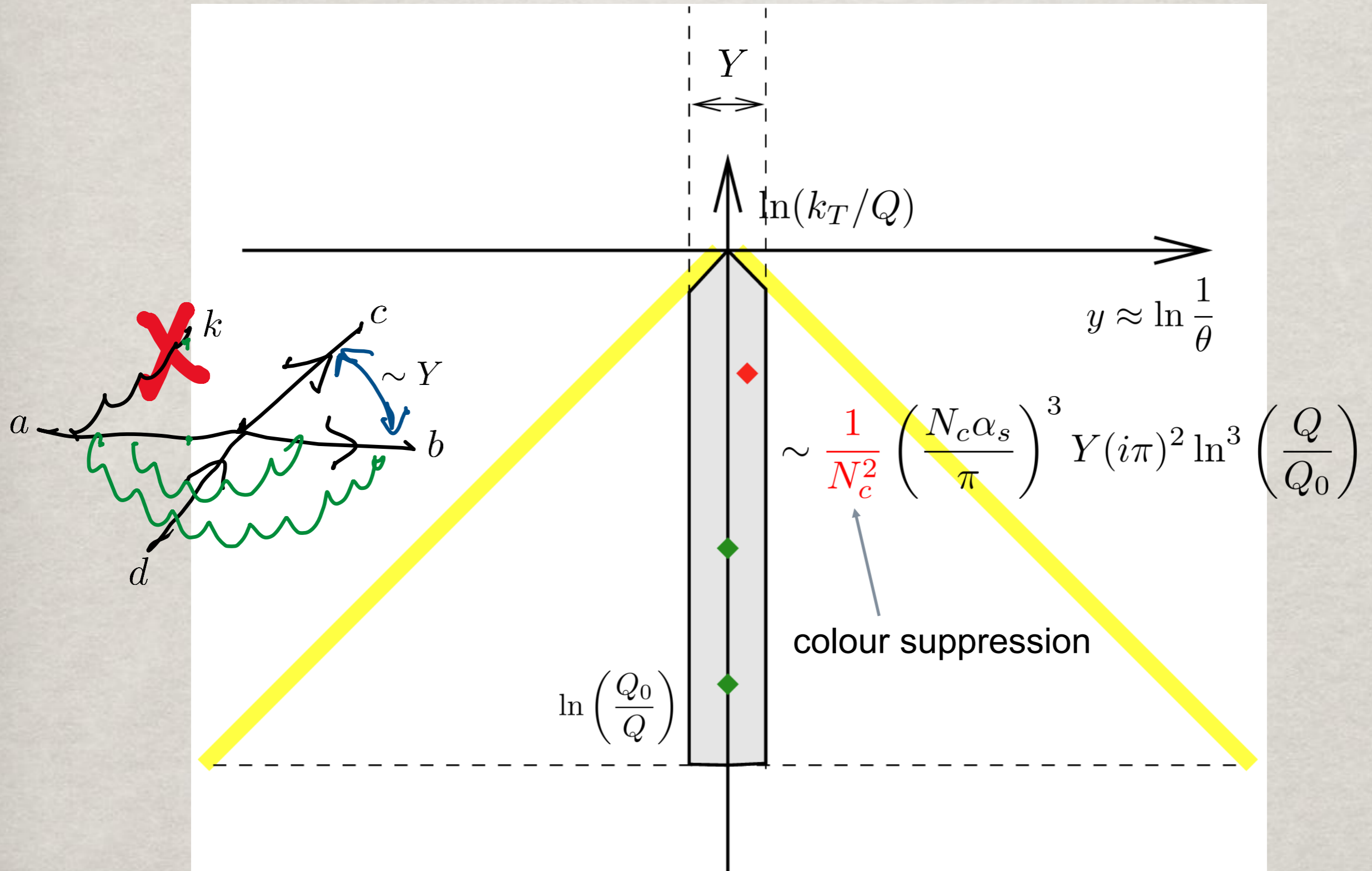
SLL IN THE LUND PLANE

Only virtual corrections survive inside the gap



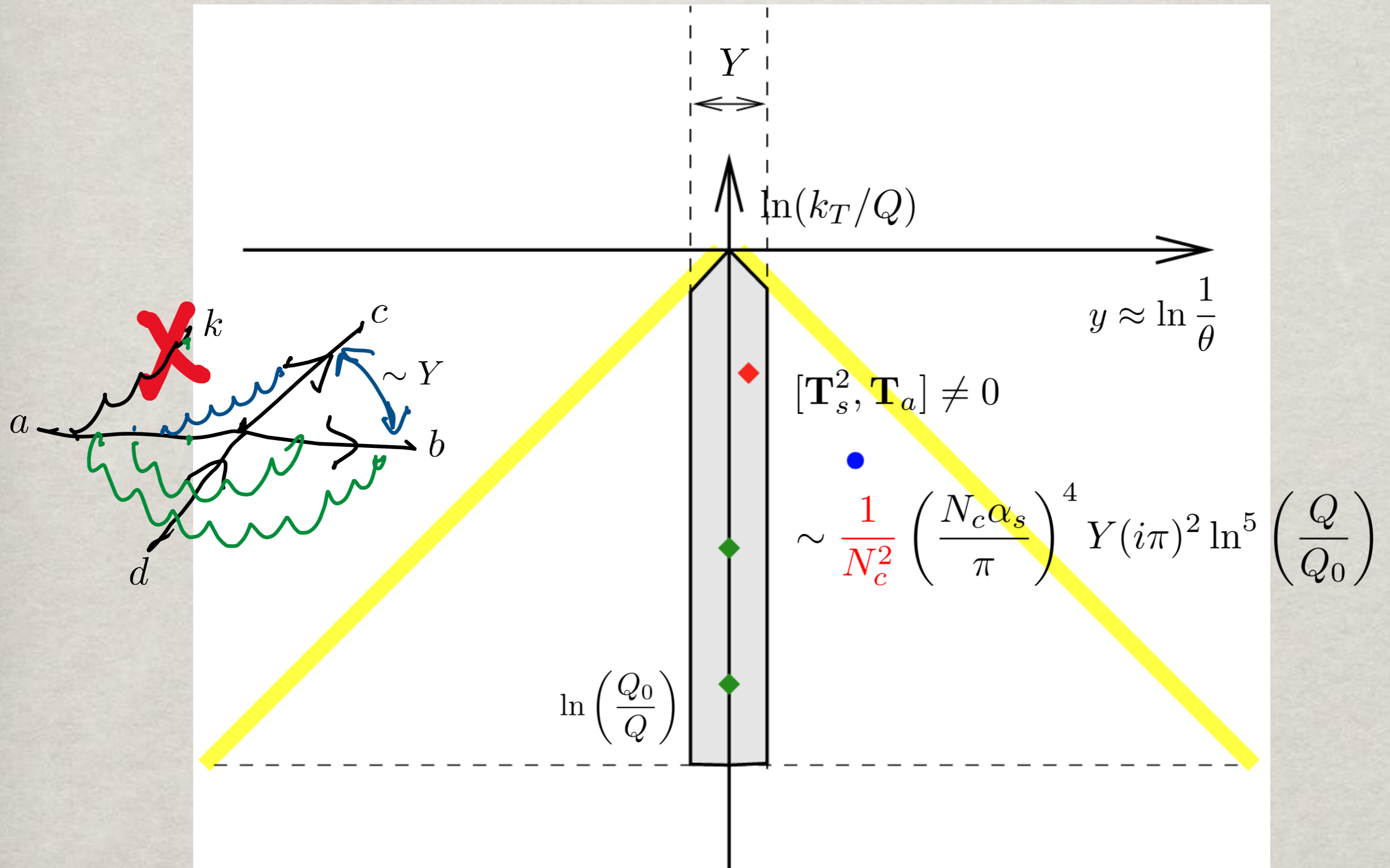
SLL IN THE LUND PLANE

Only virtual corrections survive inside the gap



SLL IN THE LUND PLANE

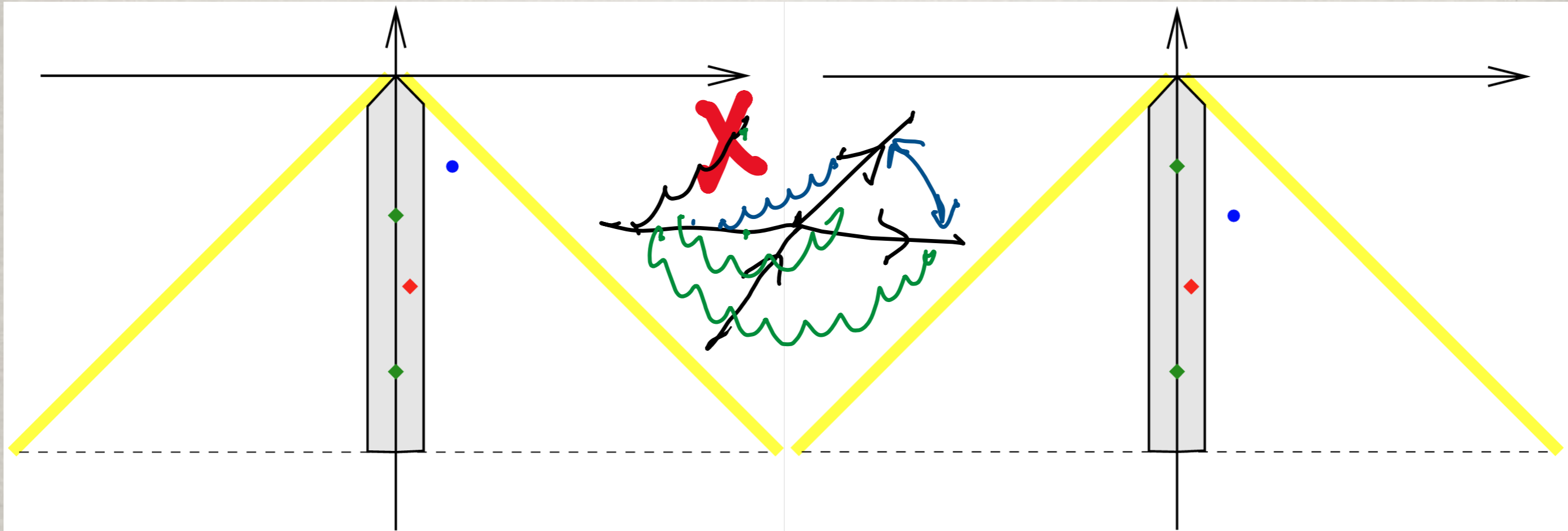
An additional collinear gluon outside the gap can be “colour trapped”



SLL AT FOURTH ORDER

hardest gluon outside the gap

second-hardest gluon outside the gap



$$\Sigma^{\text{CVL}}(Q_0) \sim \frac{A}{N_c^2} \left(\frac{N_c \alpha_s}{\pi} \right)^4 Y(i\pi)^2 \ln^5 \left(\frac{Q}{Q_0} \right)$$

[Forshaw Kyrielleis Seymour 0808.1269]

$$AN_c^2 = \text{Tr} \left([\mathbf{T}_s^2, [\mathbf{T}_s^2, \mathbf{T}_t^2]] (\mathbf{T}_a^\dagger \mathbf{H} \mathbf{T}_a - \mathbf{T}_a^2 \mathbf{H}) \right)$$

vanishes for less than 3 Born partons

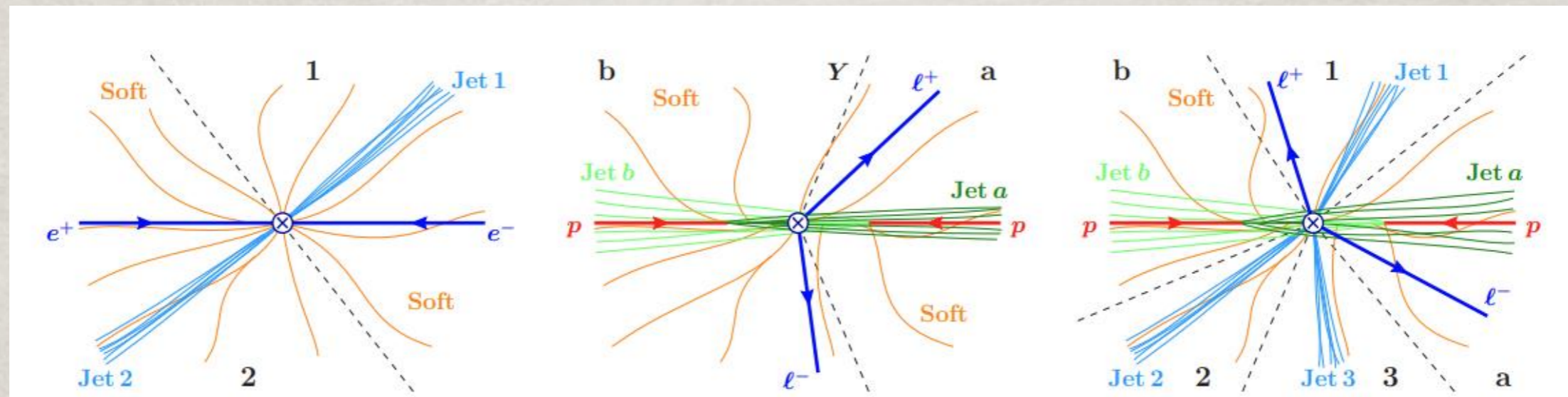
$$AN_c^2 = \text{Tr} \left([\mathbf{T}_s^2, \mathbf{T}_t^2] (\mathbf{T}_a^\dagger [\mathbf{T}_s^2, \mathbf{H}] \mathbf{T}_a - \mathbf{T}_a^2 [\mathbf{T}_s^2, \mathbf{H}]) \right)$$

vanishes for less than 4 Born partons

ONE-JETTINESS

N-JETTINESS

- Jettiness is a class of observables introduced to characterise the properties of jets
[Stewart Tackmann Waalewijn 1004.2489]
- The N-jettiness τ_N is defined in such a way that, for $\tau_N \rightarrow 0$, an event contains only N highly collimated jets



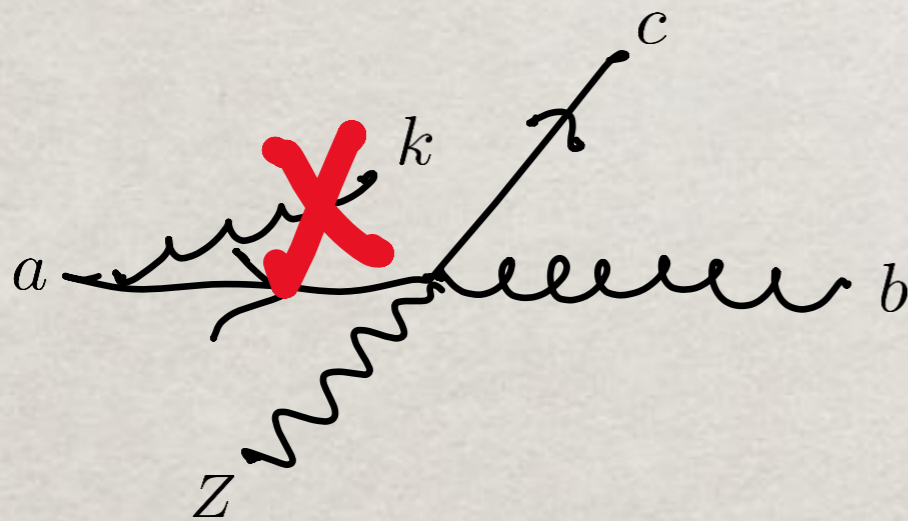
- N-jettiness is recursively IRC safe \implies with coherence, this gives access to very high (N^3 LL) accuracy in the N-jet region
[Alioli et al 2312.06496]
- Due to both its calculability and simplicity, N-jettiness is also used for
 - Isolation of exclusive N-jet events for BSM searches
[Lindert et al 1705.04664]
 - Resolution variable for phase-space slicing in NNLO calculations
[Boughezal Isgrò Petriello 1802.00456]

ONE-JETTINESS IN THE LUND PLANE

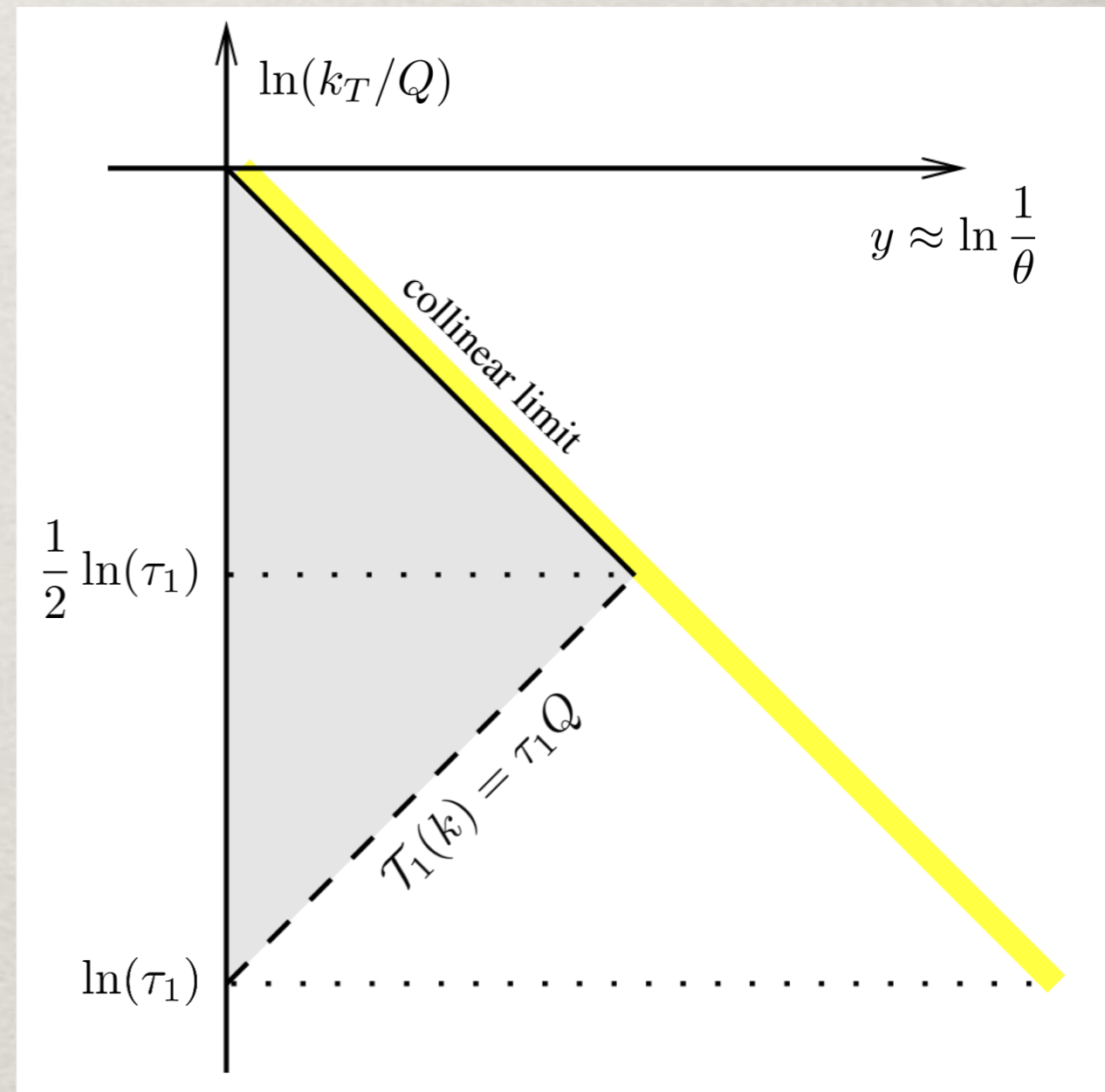
In Z+jet event, we define one-jettiness as

$$\mathcal{T}_1 \equiv \sum_i \min\{n_a \cdot k_i, n_b \cdot k_i, n_c \cdot k_i\}$$

$$\Sigma(\tau_1) = \text{Prob}(\mathcal{T}_1 < \tau_1 Q)$$

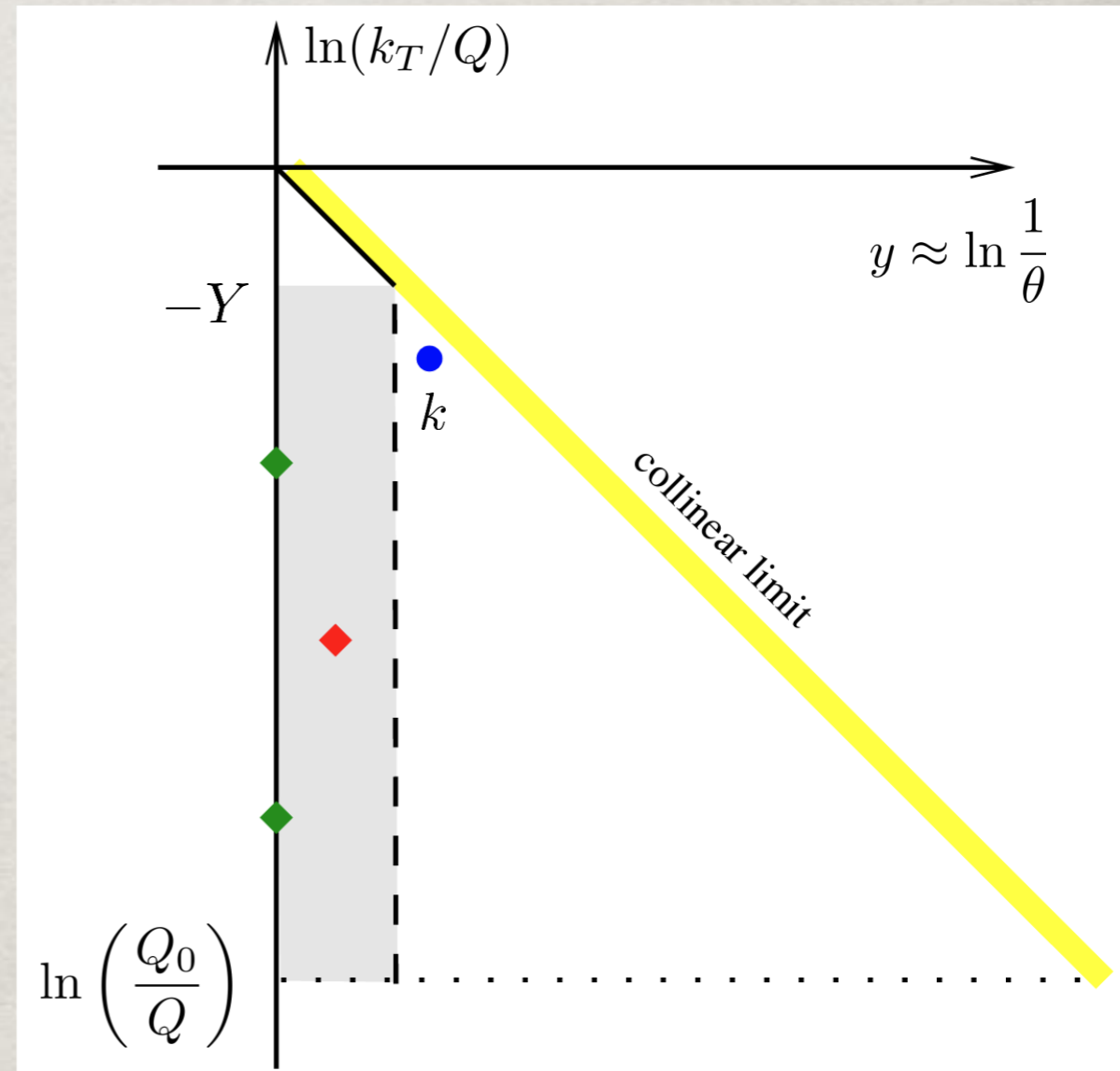
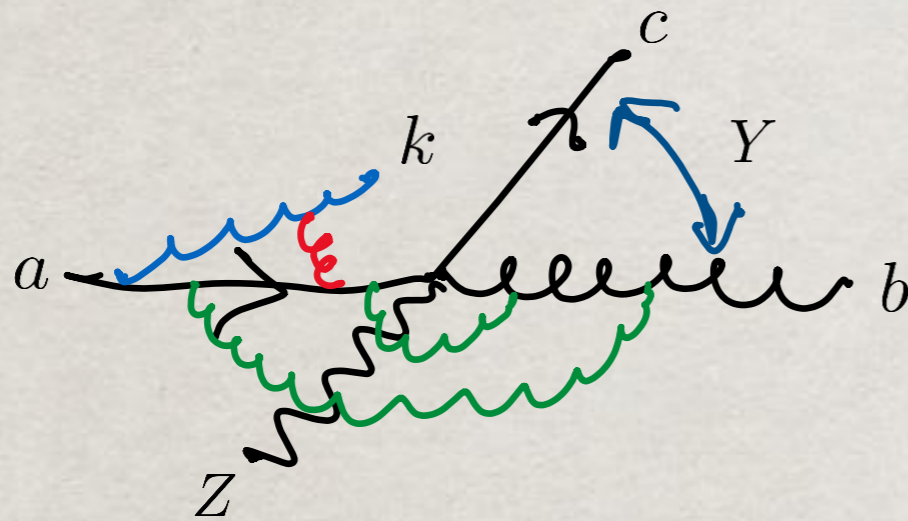


$$\Sigma(\tau_1) \sim \exp\left(- (2C_F + C_A) \frac{\alpha_s}{2\pi} L^2 + \dots\right)$$



LARGE GAP BETWEEN JETS

Let us focus on Z+jet and increase the gap between the jet and the beam...

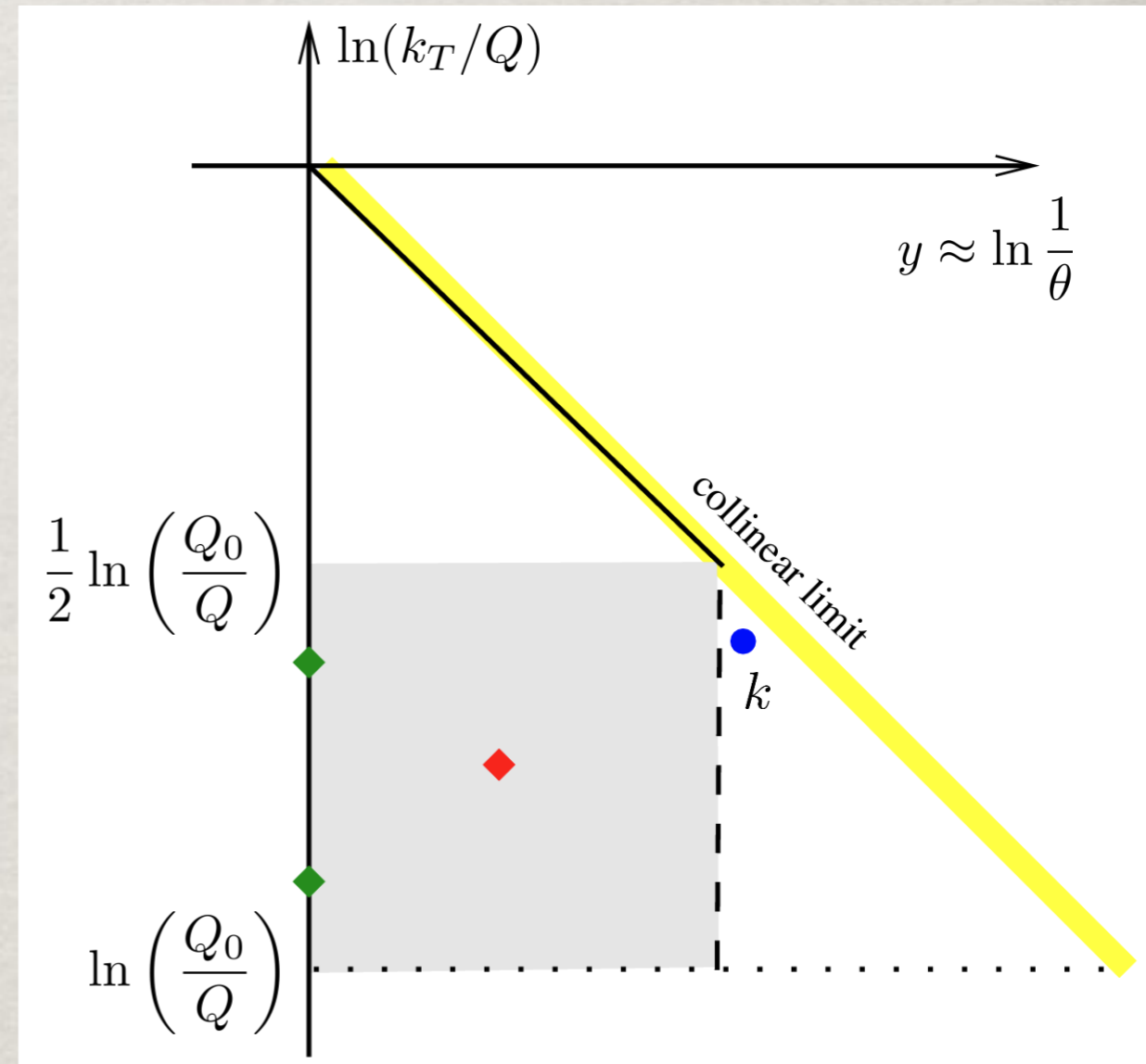
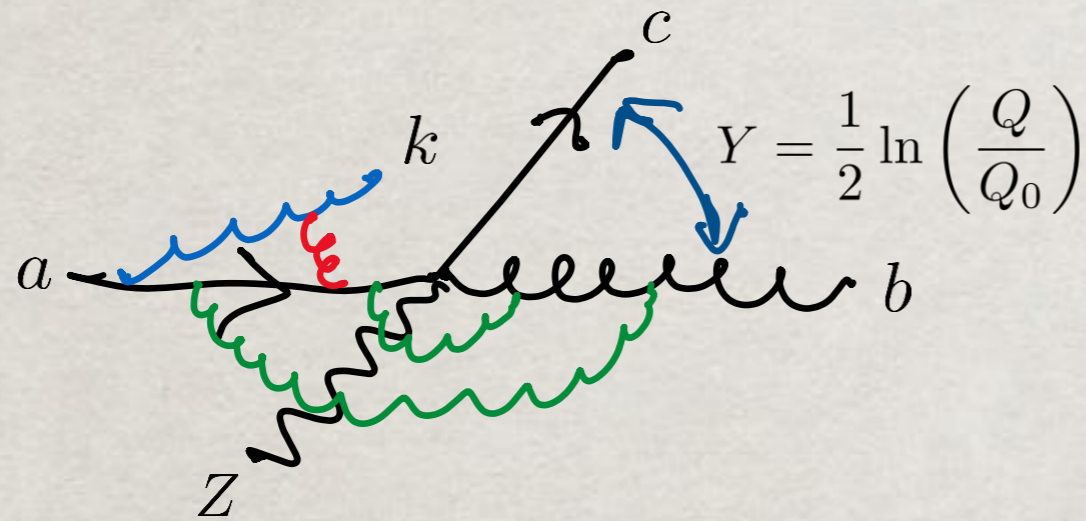


$$\Sigma^{\text{CVL}}(Q_0) = \frac{\alpha_s}{\pi} \int_{Q_0}^Q \frac{dk_T}{k_T} \int_0^{\ln(Q/k_T)} dy \Theta(y - Y) \times$$

$$\times \text{Tr} \left(\mathbf{V}_{Q_0, k_T} \mathbf{T}_a \mathbf{V}_{k_T, Q} \mathbf{H} \mathbf{V}_{k_T, Q}^\dagger \mathbf{T}_a^\dagger \mathbf{V}_{Q_0, k_T}^\dagger \right) \sim \frac{1}{N_c^2} \left(\frac{N_c \alpha_s}{\pi} \right)^4 (i\pi)^2 Y \ln^5 \left(\frac{Q}{Q_0} \right)$$

LARGE GAP BETWEEN JETS

... until it scales like the logarithm of the veto scale



$$\Sigma^{\text{CVL}}(Q_0) = \frac{\alpha_s}{\pi} \int_{Q_0}^Q \frac{dk_T}{k_T} \int_0^{\ln(Q/k_T)} dy \Theta\left(y - \frac{1}{2} \ln\left(\frac{Q}{Q_0}\right)\right) \times$$

$$\times \text{Tr}\left(\mathbf{V}_{Q_0, k_T} \mathbf{T}_a \mathbf{V}_{k_T, Q} \mathbf{H} \mathbf{V}_{k_T, Q}^\dagger \mathbf{T}_a^\dagger \mathbf{V}_{Q_0, k_T}^\dagger\right) \sim \frac{1}{N_c^2} \left(\frac{N_c \alpha_s}{\pi}\right)^4 (i\pi)^2 \ln^6\left(\frac{Q}{Q_0}\right)$$

ANALOGY WITH ONE-JETTINESS

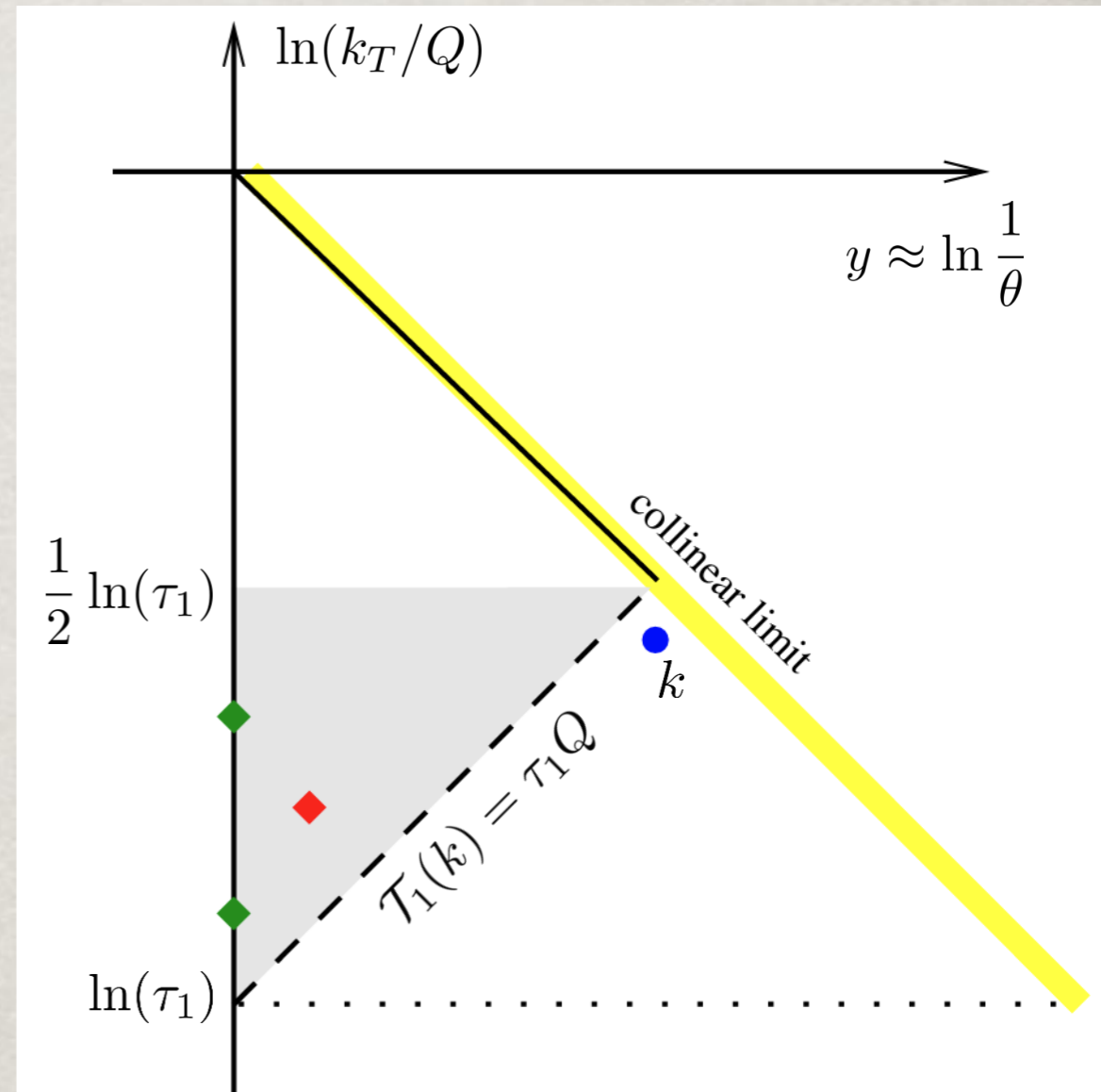
The one-jettiness constraint can be interpreted as a distorted version of the gap between jets, with a diagonal boundary

$$\mathcal{T}_1(k) = n_a \cdot k \sim k_T e^{-y}$$

$$y > \ln\left(\frac{Q}{Q_0}\right) \longrightarrow \frac{\mathcal{T}_1(k)}{Q} < \tau_1$$

⇓

$$y > \ln\left(\frac{\tau_1 k_T}{Q}\right)$$



$$\Sigma^{\text{CVL}}(\tau_1) \approx \frac{\alpha_s}{\pi} \int_{Q_0}^Q \frac{dk_T}{k_T} \int_0^{\ln(Q/k_T)} dy \Theta\left(y - \ln\left(\frac{\tau_1 k_T}{Q}\right)\right) \times$$

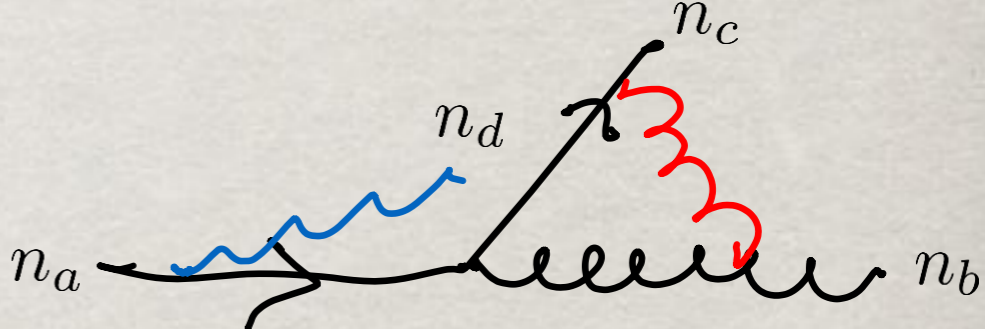
$$\times \text{Tr}\left(\mathbf{V}_{Q_0, k_T} \mathbf{T}_a \mathbf{V}_{k_T, Q} \mathbf{H} \mathbf{V}_{k_T, Q}^\dagger \mathbf{T}_a^\dagger \mathbf{V}_{Q_0, k_T}^\dagger\right) \sim \frac{1}{N_c^2} \left(\frac{N_c \alpha_s}{\pi}\right)^4 (i\pi)^2 \ln^6\left(\frac{1}{\tau_1}\right) ?$$

CVLS FOR ONE-JETTINESS

Without the collinear emission, the system is in a three-parton state

$$\mathbf{t}_i \cdot \mathbf{t}_j = \frac{1}{2}(C_i + C_j - C_k)\mathbf{1} \implies \mathbf{V}_{k_T, Q} \mathbf{H} \mathbf{V}_{k_T, Q}^\dagger = W_{k_T, Q} \mathbf{H}$$

$$\Sigma^{\text{CVL}}(\tau_1) \approx \frac{\alpha_s}{\pi} \int_{Q_0}^Q \frac{dk_T}{k_T} \int_0^{\ln(Q/k_T)} dy \Theta\left(y - \ln\left(\frac{\tau_1 k_T}{Q}\right)\right) \times$$

$$\times \text{Tr}\left(\mathbf{V}_{\tau_1 Q, k_T} \mathbf{t}_a \mathbf{H} \mathbf{t}_a^\dagger \mathbf{V}_{\tau_1 Q, k_T}^\dagger\right)$$


The additional collinear emission introduces a non-trivial four-parton colour structure

$$\mathbf{V}_{\tau_1 Q, k_T} \approx \text{Pexp} \left\{ \frac{\alpha_s}{\pi} \left[\sum_i \sum_{j \neq i} \mathbf{T}_i \cdot \mathbf{T}_j \int_{\tau_1 Q}^{k_T} \frac{dq_\perp^{(ij)}}{q_\perp^{(ij)}} \int_{-\ln Q/q_\perp^{(ij)}}^{\ln Q/q_\perp^{(ij)}} d\eta^{(ij)} \int \frac{d\phi^{(ij)}}{2\pi} \Theta(q \cdot n_{i,j} - \tau_1 Q) \right. \right.$$

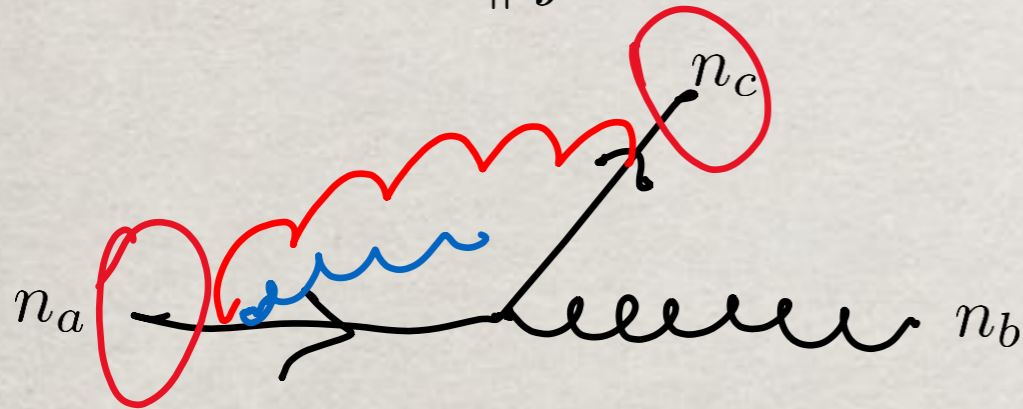
$$\left. \left. - i\pi \mathbf{T}_s^2 \ln\left(\frac{k_T}{\tau_1 Q}\right) \right] \right\}$$

CVLS FOR ONE-JETTINESS

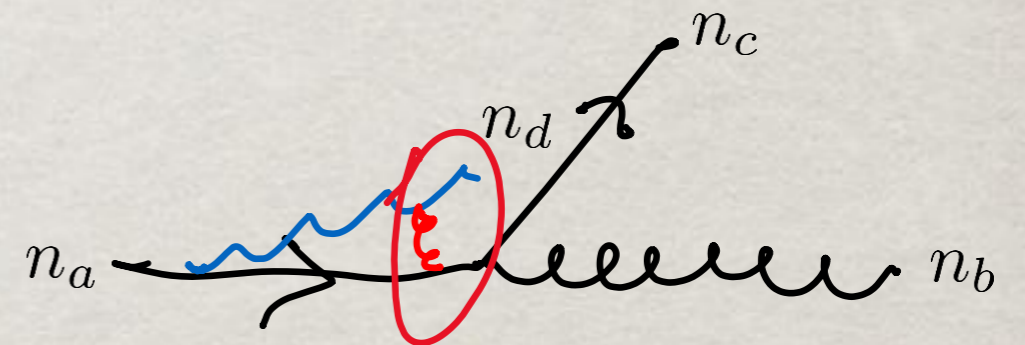
Let's take a closer look at virtual corrections

$$\mathbf{V}_{\tau_1 Q, k_T} \approx \text{Pexp} \left\{ \frac{\alpha_s}{\pi} \left[\sum_i \sum_{\substack{j \neq i \\ i \not\parallel j}} \mathbf{T}_i \cdot \mathbf{T}_j \int_{\tau_1 Q}^{k_t} \frac{dq_{\perp}^{(ij)}}{q_{\perp}^{(ij)}} \int d\eta^{(ij)} \frac{d\phi^{(ij)}}{2\pi} \Theta(q \cdot n_i - \tau_1 Q) \Theta(q \cdot n_j - \tau_1 Q) - i\pi \mathbf{T}_s^2 \ln \left(\frac{k_T}{\tau_1 Q} \right) \right] \right\}$$

$i \not\parallel j$



$i \parallel j$



$$\int_{q \cdot n_{i,j} > \tau_1 Q} d\eta^{(ij)} \frac{d\phi^{(ij)}}{2\pi} \approx \ln \left(\frac{q_{\perp}^2}{\tau_1 Q^2} \frac{n_i \cdot n_j}{2} \right)$$

$$\int_{q \cdot n_{i,j} > \tau_1 Q} d\eta^{(ij)} \frac{d\phi^{(ij)}}{2\pi} \rightarrow 0 \quad (\tau_1 \rightarrow 0)$$

$$\sum_i \sum_{\substack{j > i \\ j \not\parallel i}} \mathbf{T}_i \cdot \mathbf{T}_j = -\frac{1}{2} \sum_i \mathbf{T}_i^2 - \mathbf{T}_a \cdot \mathbf{T}_d \equiv \mathbf{T}_{ad}^2$$

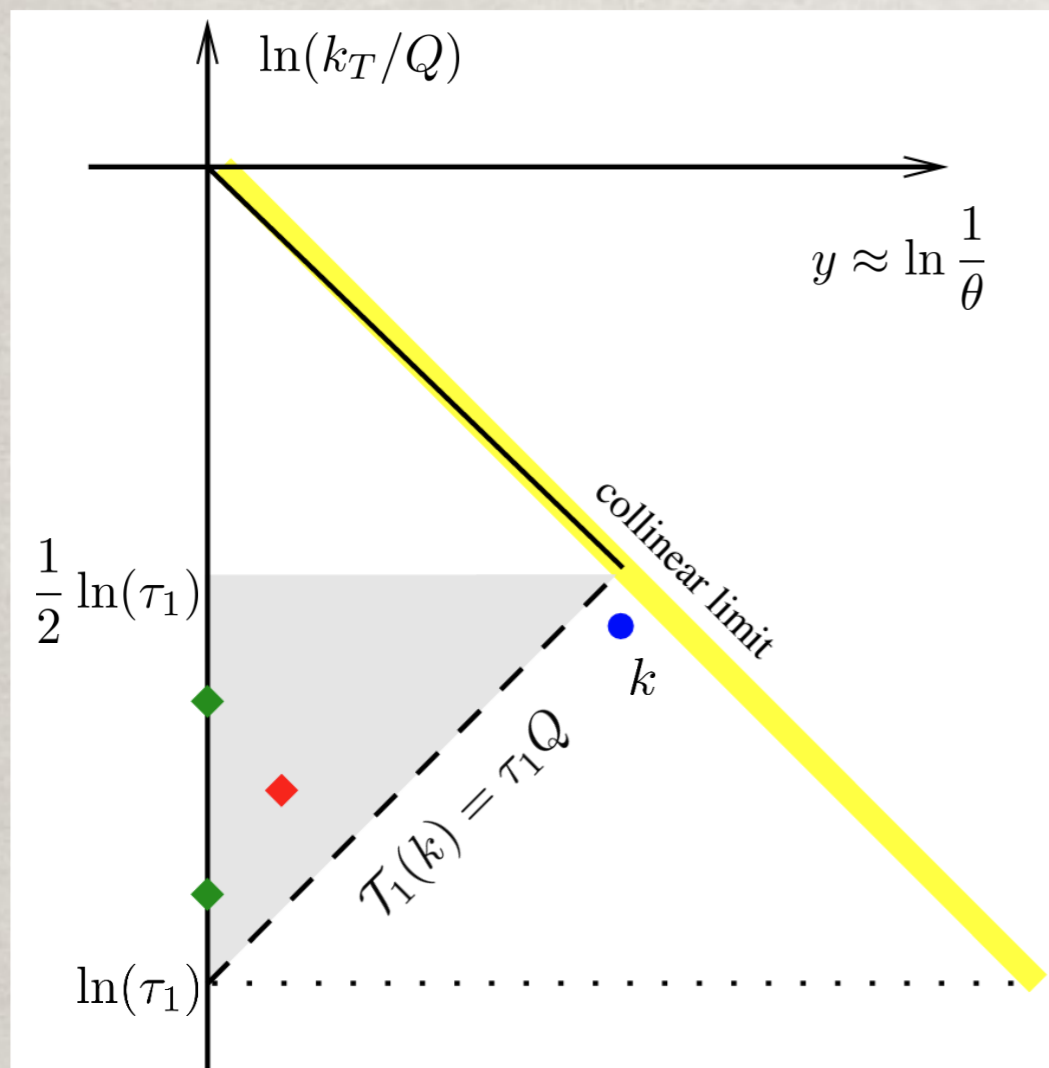
$$\mathbf{V}_{\tau_1 Q, k_t} \approx \exp \left(\frac{\alpha_s}{\pi} \left[\mathbf{T}_{ad}^2 \ln^2 \left(\frac{k_T}{\tau_1 Q} \right) - i\pi \mathbf{T}_s^2 \ln \left(\frac{k_T}{\tau_1 Q} \right) \right] \right)$$

SUPER-SUPER LEADING LOGARITHMS

For one-jettiness, coherence violating logarithms are super-super-leading

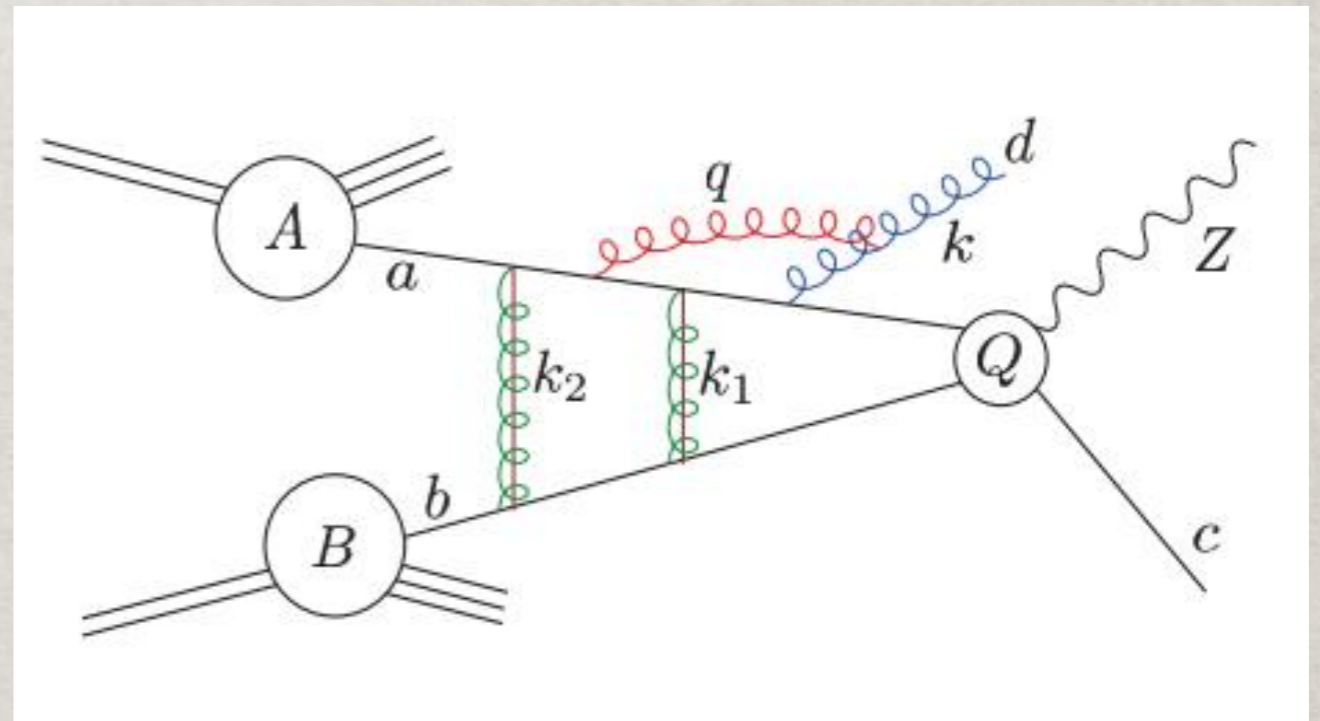
[AB Forshaw Holguin 2511.11799]

$$\Sigma_{a=q,g}^{\text{CVL}}(\tau_1) = \frac{A_a^2}{N_c} \left(\frac{N_c \alpha_s}{\pi} \right)^4 \int_{\tau_1 Q}^Q \frac{dk_T}{k_T} \int_{k_T/Q}^1 \frac{d\theta}{\theta} \Theta(\tau_1 Q - k_T \theta) \ln^2 \left(\frac{k_T}{\tau_1 Q} \right) \left(-i\pi \ln \left(\frac{k_T}{\tau_1 Q} \right) \right)^2$$



$$A_q = \frac{8}{3} T_R^4$$

$$A_g = -\frac{32}{3} T_R^4$$

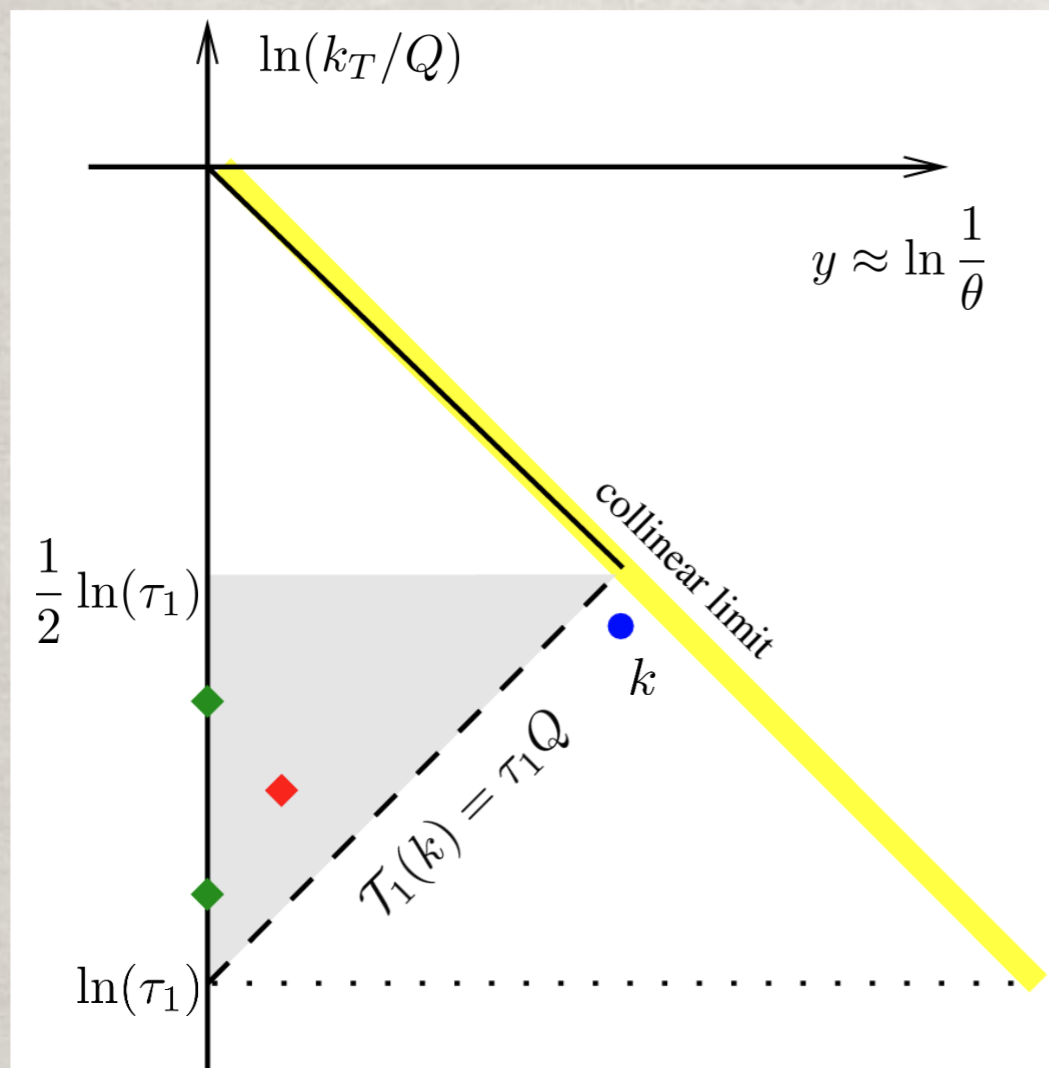


SUPER-SUPER LEADING LOGARITHMS

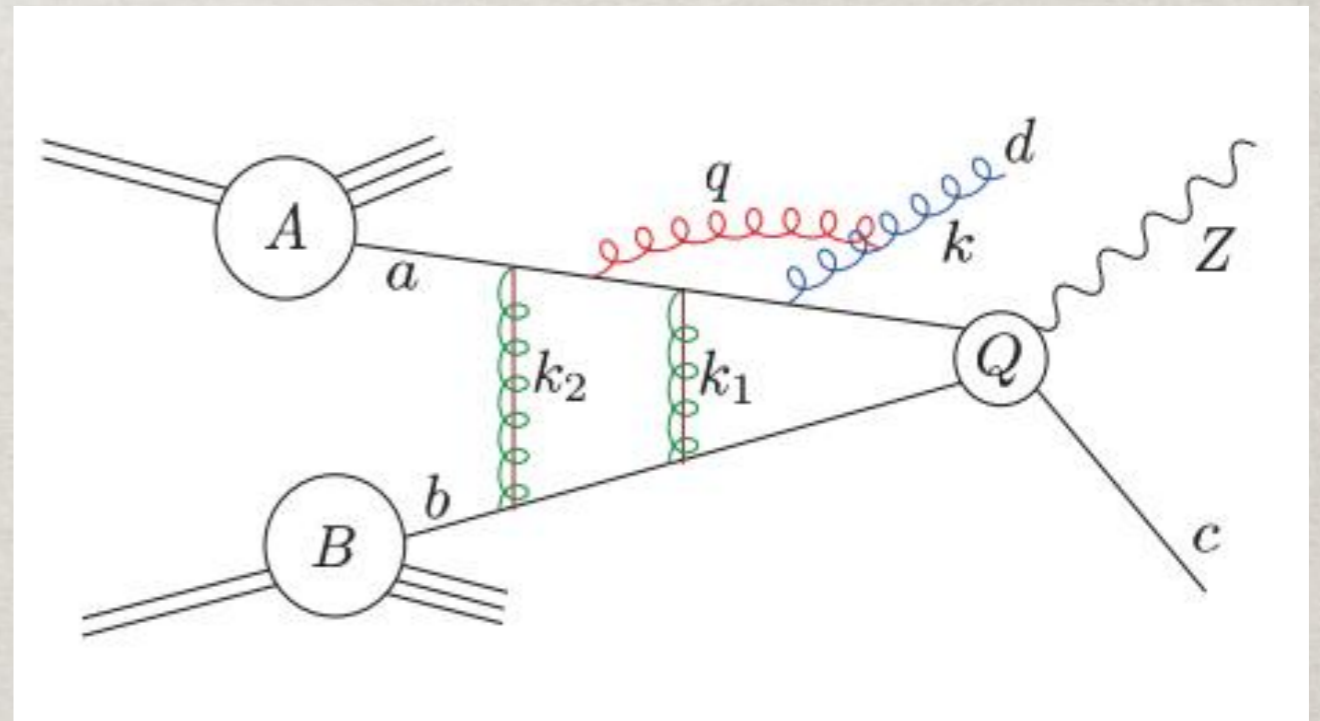
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$$\Sigma_a^{\text{CVL}}(\tau_1) = \frac{A_a}{N_c^2} \left(\frac{N_c \alpha_s}{\pi} \right)^4 \frac{(-i\pi)^2}{480} \left(\ln \frac{1}{\tau_1} \right)^6 \sim \alpha_s^4 L^6$$

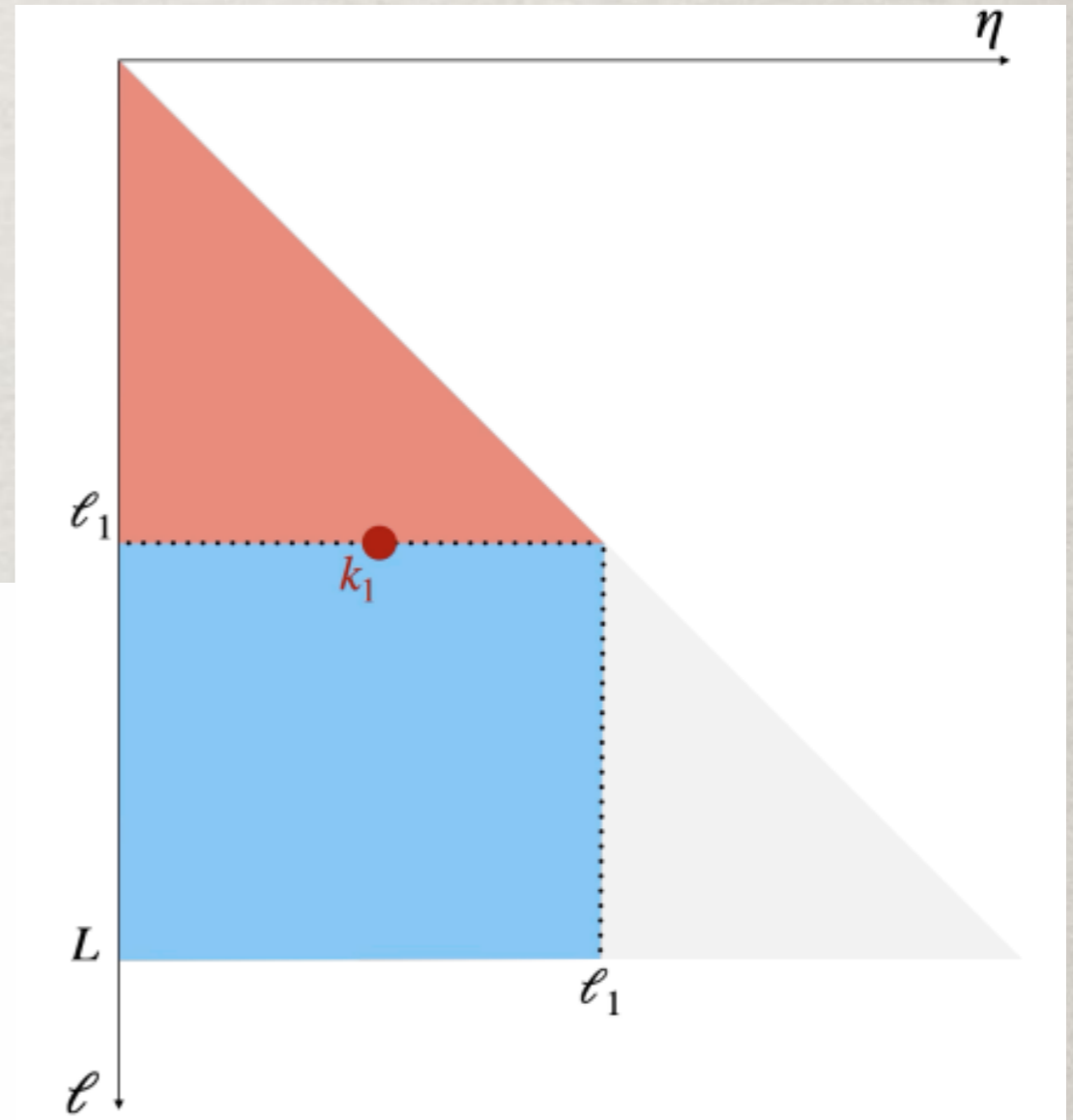
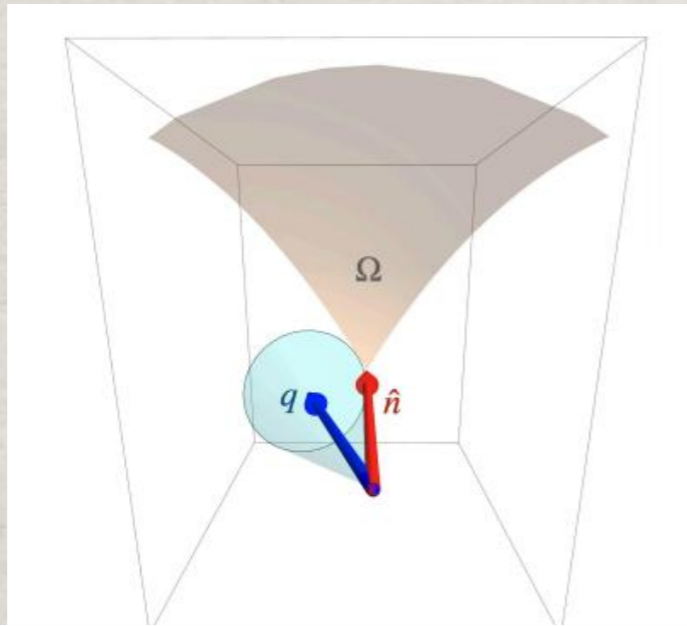


This result has been confirmed using EFT techniques

[Becher Hager Neubert Schwienbacher 2603.12383]

TRANSVERSE ENERGY FLOW

Super-super leading logarithms have been found also in the transverse energy flow into an azimuthal patch of size $\Delta\phi = 2\pi f$ [Dasgupta Fraley Monni Nabeebaccus 2511.14681]



$$\hat{\sigma}_{\text{CVL}} = \left(-\frac{2\alpha_s}{\pi}\right)^5 (1-f)^2 \int_{E_T}^Q \frac{dk_{t,3}}{k_{t,3}} \int_{-\eta_3^{\max}}^{\eta_3^{\max}} d\eta_3 \int_{E_T}^{k_{t,3}} \frac{dk_{t,4}}{k_{t,4}} \int_{-\eta_4^{\max}}^{\eta_4^{\max}} d\eta_4 \int_{E_T}^{k_{t,4}} \frac{dk_t}{k_t} \left[\frac{1}{3} \ln^2 \left(\frac{k_{t,4}}{E_T} \right) \langle m_0 | \mathbf{D}_{a_3,(2)}^{\mu_3 \dagger} \mathbf{D}_{a_4,(3)}^{\mu_4 \dagger} \left[\Gamma_{(4)}^I, \left[\Gamma_{(4)}^I, \Gamma_{(4)}^R \right] \right] \mathbf{D}_{a_4,(3)}^{\mu_4} \mathbf{D}_{a_3,(2)}^{\mu_3} | m_0 \rangle \right]$$

$$\Sigma_{\text{DY}}^{\text{CVL}} = -\frac{1}{N_c^2} \frac{C_F}{N_c} \left(\frac{N_c \alpha_s}{\pi} \right)^5 f(1-f) \frac{L^8}{180}$$

In DY, one needs two collinear emissions to have a non-trivial colour structure \implies CVLs start at $(\alpha_s L)^2 (\alpha_s L)^3 = \alpha_s^5 L^8$

AVENUES FOR RESUMMATION

SLL RESUMMATION

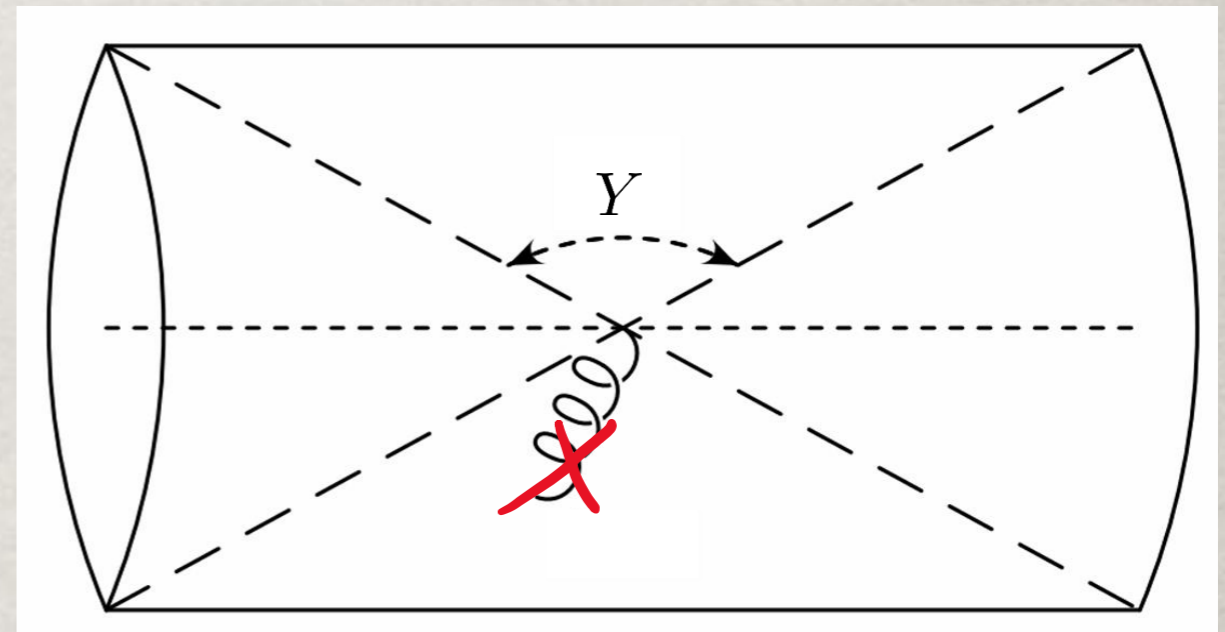
The gap-between-jets (GBJs) cross section admits an all-order factorisation formula

[Becher Neubert Shao 2107.01212]

$$\frac{d\sigma}{dY} = \int dx_a dx_b \sum_{n=2+J}^{\infty} \langle \mathcal{H}_m(\{\underline{n}\}, Q, x_a, x_b, \mu) \otimes \mathcal{W}_m(\{\underline{n}\}, Q_0, x_a, x_b, \mu) \rangle$$

Resummations of logarithms of $Q_0 \iff$
RGE equation for the hard functions \mathcal{H}_m

$$\mu \frac{d}{d\mu} \mathcal{H}_m(Q, \mu) = - \sum_{l=2}^m \mathcal{H}_l(Q, \mu) \otimes \Gamma_{lm}$$



$$\Gamma^{(1)}(x_a, x_b) = \delta(1 - x_a)\delta(1 - x_b)\Gamma^S + \text{hard collinear part}$$

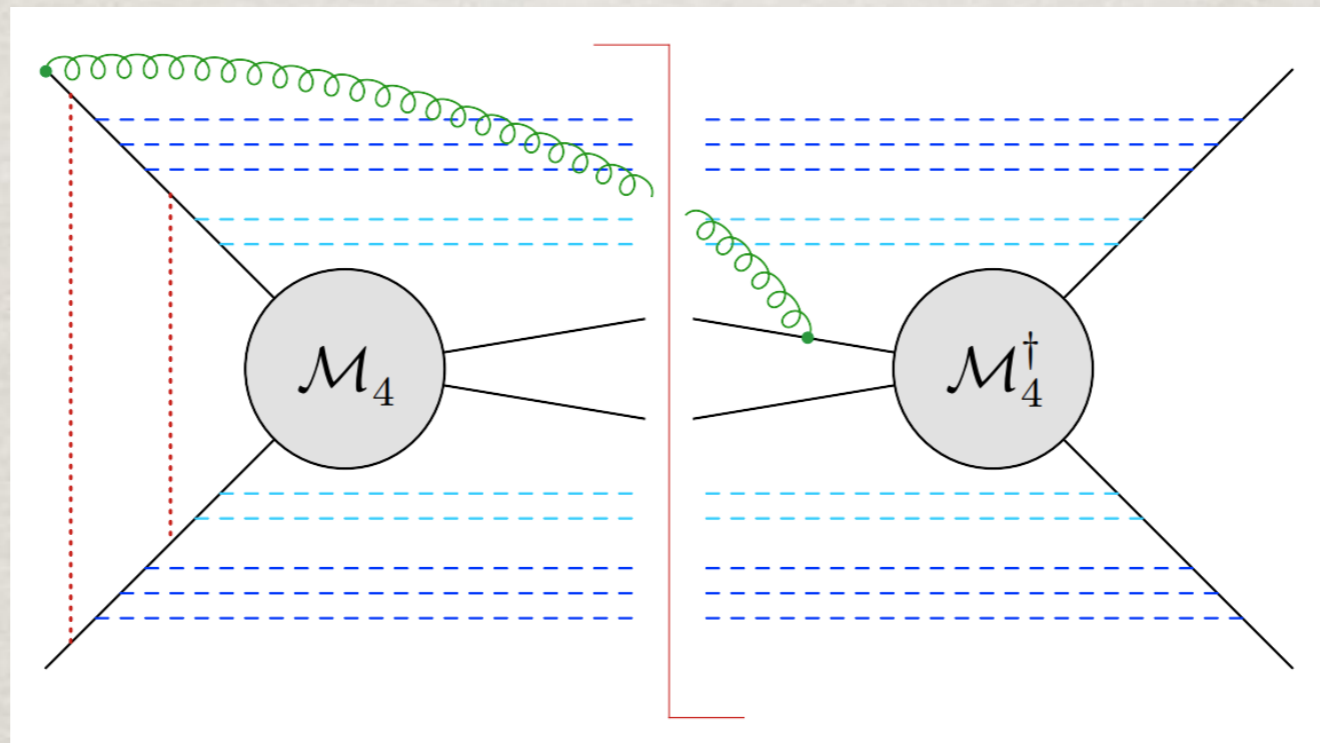
$$\Gamma^S = \bar{\Gamma} + \Gamma^G + \Gamma^c \ln \frac{\mu^2}{\hat{s}}$$

wide-angle Glauber collinear

SLL RESUMMATION

The largest super-leading logarithms can be obtained by resumming collinear emissions at all orders

[Becher Neubert Shao 2107.01212]



$$L \equiv \ln(Q/Q_0)$$

$$\langle \mathcal{H}_4(\Gamma^c)^r \Gamma^G (\Gamma^c)^{n-r} \Gamma^G \bar{\Gamma} \rangle \rightarrow (\pi^2 (\alpha_s L)^2) (N_c \alpha_s L^2)^n (N_c Y \alpha_s L)$$

The all-order resummation can be expressed in term of seven colour structures

[Becher Neubert Shao Stillger 2307.06359]

$$\hat{\sigma}_{2 \rightarrow M}^{\text{SLL}} \sim \frac{1}{N_c^2} (\pi^2 Y) (N_c \alpha_s L)^3 \left[k_0 \Sigma_0(N_c \alpha_s L^2) + \sum_{i=1}^6 k_i \Sigma(v_i, N_c \alpha_s L^2) \right]$$

GENERAL STRUCTURE OF CVLS

Coherence violating logarithms have a different structure according to the considered class of observables

- At least two Coulomb gluons must be present
- Collinear emissions must always be resummed

Observable	Soft virtual gluons	Colour space	Logarithms
Gap between jets	One is enough	Grows with the number of soft virtual gluons	SLL $\alpha_s^n L^{2n-3}$
N-jet rIRC safe	Must be resummed if rapidity suppressed (e.g. one-jettiness)	N+4 parton-like	SSLL $\alpha_s^n L^{2n-2}$
Interjet energy flow	Must be resummed	Grows with the number of soft virtual gluons	SSLL $\alpha_s^n L^{2n-2}$

CONCLUSIONS

- Coherence is an important property of QCD radiation
- Coulomb gluons transfer colour between initial-state partons, thus modifying the structure of initial-state collinear splitting
- Coherence violations lead to super-leading logarithms in non-global observables
- Global observables can be affected by coherence-violating super-super-leading logarithms

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Two main areas of research

- Show with explicit calculations that collinear factorisation still holds
- Perform the resummation of coherence-violating logarithms

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Thank you for your attention!

EXTRA

RECOVERING COLLINEAR FACTORISATION

Below the scale Q_0 there is no constraint on real emissions

[Forshaw Holguin 2109.03665]

$$\frac{\alpha_s}{\pi} \int_{\mu_F}^{Q_0} \frac{dk_T}{k_T} \int_0^{\ln(Q/k_T)} dy f_a(x_a, \mu_F) f_b(x_b, \mu_F) \times$$

$$\times \left[\text{Tr} \left(\mathbf{V}_{\mu_F, k_T} \mathbf{T}_a \mathbf{V}_{k_T, Q_0} \mathbf{H}(Q_0, Q) \mathbf{V}_{k_T, Q_0}^\dagger \mathbf{T}_a^\dagger \mathbf{V}_{\mu_F, k_T}^\dagger \right) - C_F \text{Tr} \left(\mathbf{V}_{\mu_F, Q_0} \mathbf{H}(Q_0, Q) \mathbf{V}_{\mu_F, Q_0}^\dagger \right) \right]$$

⇓

We replace the soft matrix element with the full splitting function

$$\frac{\alpha_s}{\pi} \int_{\mu_F}^{Q_0} \frac{dk_T}{k_T} \int_0^{1-k_T/Q} dz \left(\frac{1+z^2}{1-z} \right) f_b(x_b, \mu_F) \times$$

$$\times \left[\text{Tr} \left(\mathbf{V}_{\mu_F, k_T} \mathbf{T}_a \mathbf{V}_{k_T, Q_0} \mathbf{H}(Q_0, Q) \mathbf{V}_{k_T, Q_0}^\dagger \mathbf{T}_a^\dagger \mathbf{V}_{\mu_F, k_T}^\dagger \right) \frac{1}{z} f_a \left(\frac{x_a}{z}, \mu_F \right) \Theta(z - x_a) \right.$$

$$\left. - C_F \text{Tr} \left(\mathbf{V}_{\mu_F, Q_0} \mathbf{H}(Q_0, Q) \mathbf{V}_{\mu_F, Q_0}^\dagger \right) f(x_a, \mu_F) \right]$$

RECOVERING COLLINEAR FACTORISATION

$$\frac{\alpha_s}{\pi} \int_{\mu_F}^{Q_0} \frac{dk_T}{k_T} \int_0^{1-k_T/Q} dz \left(\frac{1+z^2}{1-z} \right) f_b(x_b, \mu_F) \times$$

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$$\left. - C_F \text{Tr} \left(\mathbf{V}_{\mu_F, Q_0} \mathbf{H}(Q_0, Q) \mathbf{V}_{\mu_F, Q_0}^\dagger \right) f(x_a, \mu_F) \right]$$

Virtual correction contain only Coulomb phases

$$\mathbf{V}_{Q_1, Q_2} \approx \text{Pexp} \left\{ -\frac{\alpha_s}{\pi} \ln \left(\frac{Q_2}{Q_1} \right) \left[\mathbf{T}_t^2 \underbrace{Y}_{=0} + i\pi \mathbf{T}_s^2 \right] \right\} \implies \mathbf{V}_{Q_1, Q_2} \mathbf{V}_{Q_1, Q_2}^\dagger = \mathbf{1}$$

Together with the lowest order contribution, this gives

$$\underbrace{\text{Tr}(\mathbf{H}(Q_0, Q))}_{=\Sigma(Q_0)} f_b(x_b, \mu_F) \underbrace{\left[f(x_a, \mu_F) + \frac{\alpha_s}{\pi} \int_{\mu_F}^{Q_0} \frac{dk_T}{k_T} \int_{x_a}^1 \frac{dz}{z} C_F \left(\frac{1+z^2}{1-z} \right)_+ f \left(\frac{x_a}{z}, \mu_F \right) \right]}_{\approx f(x_a, Q_0)}$$

Unresolved real emissions reconstruct the pdfs at the veto scale Q_0

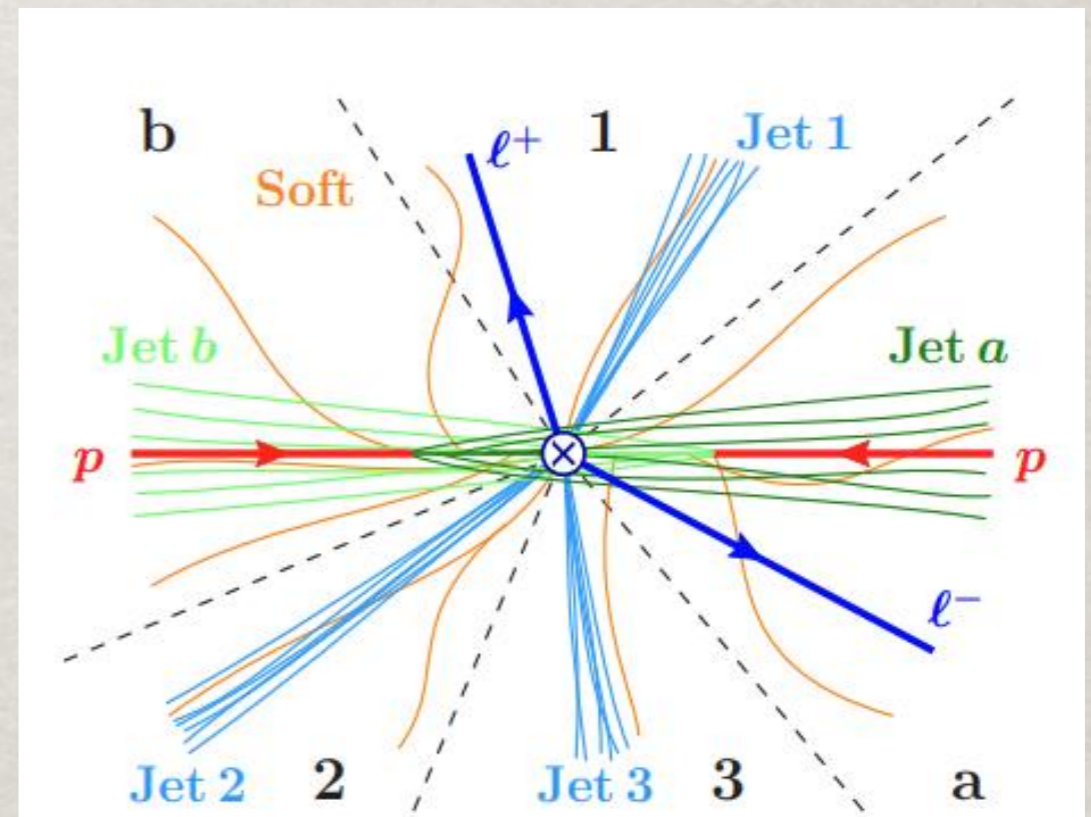
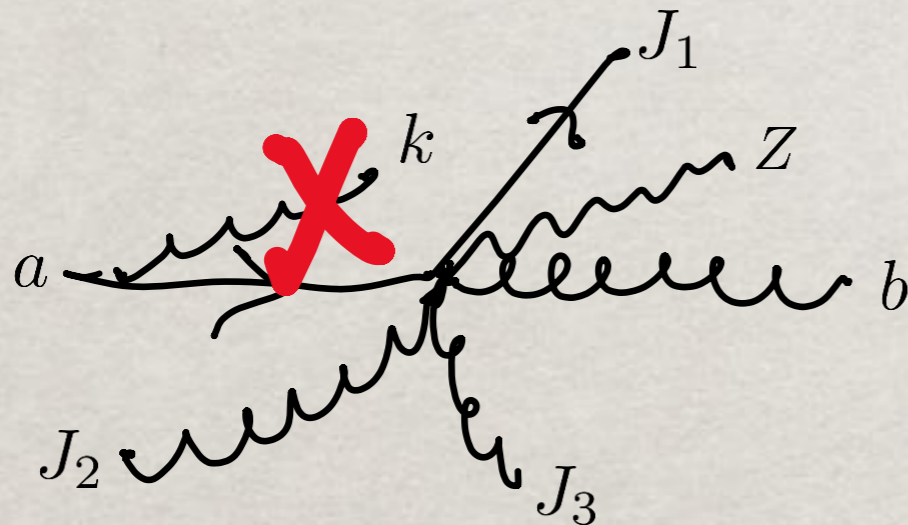
[Becher Hager Jaskiewicz Neubert Schwienbacher 2408.10308]

FACTORISATION THEOREM

In general, one can define N-jettiness as

$$\mathcal{T}_N \equiv \sum_i \min \left\{ \frac{p_a \cdot k_i}{Q_a}, \frac{p_b \cdot k_i}{Q_b}, \frac{p_{J_1} \cdot k_i}{Q_1}, \dots, \frac{p_{J_N} \cdot k_i}{Q_N} \right\}$$

$$\Sigma(\tau_N) = \text{Prob}(\mathcal{T}_N < \tau_N Q)$$



Neglecting Coulomb gluons, N-jettiness obeys an all-order factorisation

$$\frac{d\Sigma(\tau_N)}{d\tau_N} \sim \underbrace{\langle B_a \otimes B_b \otimes J_1 \otimes \dots \otimes J_N \rangle}_{\text{numbers}} \otimes \underbrace{\langle \mathcal{S}_N \otimes \mathcal{H}_N \rangle}_{\text{colour matrices}}$$

[Stewart Tackmann Waalewijn 1004.2489]